Sale of Visas: A Smuggler’s Final Song?

Emmanuelle Auriol and Alice Mesnard
SALE OF VISAS: A SMUGGLER’S FINAL SONG?

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Abstract

Is there a way of eliminating human smuggling? We set up a model to simultaneously determine the provision of human smuggling services and the demand from would-be migrants. A visa-selling policy may be successful at eliminating human smugglers by eroding their profits but it necessarily increases immigration. In contrast, re-enforced repression decreases migration but uses the help of cartelized smugglers. To overcome this trade-off we study how legalisation and repression can be combined to eliminate human smuggling while controlling migration flows. This policy mix also has the advantage that the funds raised by visa sales can be used to finance additional investments in border and internal controls (employer sanctions and deportations). Simulations of the policy implications highlight the complementarities between repression and legalisation and call into question the current policies.

JEL Classifications: F22, I18, L51, O15.

Key words: migration, migration policies, market structure, legalisation, human smuggling.

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1 Introduction

Human smuggling entails huge costs for societies. First, it is a dangerous operation, which frequently results in the death of those involved. Each year, an estimated 2,000 people are drowned in the Mediterranean on their journey from Africa to Europe (The Economist, August 06, 2005) and many more on other routes. Even when migrants are successful at reaching destination areas, they are often exploited in transit and destination countries and deprived of economic and human rights due to their illegal status (see for example Poulin, 2005 on prostitution and human trafficking or Human Rights Watch, 2000, on bonded labour in sweatshops).\(^1\) Second, crossing borders illegally entails very high financial costs. For border crossings such as from Mexico into the United States, human smugglers can charge up to $4,000, while trans-Pacific crossings of Chinese immigrants into the United States cost above $35,000 in the mid 90s and have since increased sharply.\(^2\) This makes people smuggling a lucrative business. As of 2003, it brought over $5 billion revenues a year in the US and around €4 billion in the EU (Padgett, 2003).\(^3\) Finally, over the years, human smuggling has integrated with other types of illegal and lucrative transnational activities such as drug shipping and prostitution. Led by international criminal organizations they pose a threat to the rule of law in countries of origin, transit, and destination.

Although it is important for policy makers to understand why such illegal activities and their associated criminalities are so prevalent, there are surprisingly very few studies on the supply side of illegal migration (noticeable exceptions

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1. Trafficking victims coming from 127 countries have been found in 137 countries around the world. It is estimated that there are at least 2.4 million persons who are the victims of trafficking at any time. The most visible form of exploitation is for sexual purposes and approximately 79% of trafficking victims are trafficked for sexual exploitation, with 18% being trafficked for forced labour. While it is difficult to ascertain, it is estimated that over US$30 billion are generated in profits by trafficked persons every year (UNODC 2012).


3. The annual associated flows of smuggled immigrants are estimated to be at around 350,000 in the US and 800,000 in the EU (The Economist 6 August 2005). These rough estimates should be dealt with caution as reliable data on such illegal activity are difficult to obtain.
are Friebel and Guriev, 2006 and Tamura, 2010, as surveyed by Mahmoud and Trebesch, 2010). The paper contributes to this new literature by, first, studying the industrial organization of human smuggling, notably smugglers pricing and supply of services, and second, exploring what type of economic policies can be implemented to fight against them.

Current migration policies, which combine quotas on visas with repression of illegal migration, are very ineffective instruments to fight against the illegal migration business. In fact, strong restrictions on labour mobility imply that many candidates are obliged to arrange long distance migration with the help of intermediaries who organise air, sea or ground transportation and provide them with forged documents, clothes, food and accommodation during the trip (de Haas, 2006). Empirically, the question as to whether repressive measures are effective at decreasing the number of illegal migrants is still very much debated. It is indeed difficult to obtain good data on illegal migration and to identify the causal impact of the policies. In spite of these difficulties a few empirical papers investigate the determinants of illegal migration and attempt to assess its responsiveness to border enforcement measures (Donato et al., 1992, Massey and Espinosa, 1997, Hanson and Spilimbergo, 1999, Hanson et al., 2002, Angelucci 2004). To our knowledge, all existing evidence on illegal migration focuses on cross border migration between the US and Mexico and points to a small or insignificant effect of stricter deportation rules and stricter border controls after the Immigration Reform and Control Act (for a review see Hanson, 2006). For example, using detailed data on cross-border trips of illegal workers from the Mexican Migration Project, Gathman (2008) shows that the price elasticity of demand for illegal migration is relatively small: when the price to cross the border with the help of coyotes increases, migrants may choose to migrate by

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4Illegal migration represents a sizeable proportion of the foreign population living in high wages countries. In Europe for example, the Clandestino Research Project estimates that 1.8 to 3.3 million irregular foreign residents live in the old Member States of the EU15 in 2008 (See at: http://clandestino.eliamep.gr/ or Dustmann and Frattini, 2011). This represents 0.46% to 0.83% of their population and 7% to 12% of their foreign population. Worldwide, the International Labour Organisation estimates that 10 to 15 per cent of migration today involves migration under irregular situations i.e. entering or working in countries without authorization (http://www.ilo.org/public/libdoc/ilo/2006/106B09_492_engl.pdf).
their own means and forego the services of smugglers by taking additional risks to cross the border in more remote areas.

However, we expect long distance migration to respond more strongly to smugglers’ prices as it is not feasible without their services. Although there is no evidence on the price elasticity of long haul illegal migration, we know from history that long distance legal migration responded strongly to changes in the market structure of shipping cartels at the beginning of the 20th century. This has been tested empirically by Deltas et al (2008), who show that the existence of relatively tight, well-organized cartels restricted the flow of transatlantic migrants below what would have occurred in a more competitive environment. Today, illegal migration still entails sizeable costs, which may continue to be prohibitively expensive for poor workers and may depend strongly on the industrial organisation of smugglers.

Since repressive policies are ineffective at eliminating smugglers, this paper focuses on what would happen if a government used basic economic tools, such as price schemes, to fight them by offering candidates the option to pay a fee to cross the border legally. The idea of selling migration visas to regulate migration flows is not new: policy proposals have already fed many debates in the general press, blogs and policy reports (see Becker, 2002, the Becker-Posner blog of 31rst July 2005, Freeman, 2006, Orrenius and Zavodny 2010, Saint Paul, 2009 and early discussions by Simon, 1989), and been strongly criticised by other economists such as A.Banerjee or S.Mullainathan (The Economist, 26 June 2010). The opponents of such legalisation argue that the sale of visas may generate a new type of bonded labour between indebted migrants and their employers and that the market does not necessarily allocate resources efficiently. The proponents of legalisation argue that, instead of fuelling the mafia by restricting migration, governments should collect money by selling visas (for instance through auctions). Indeed a business can only be controlled and taxed if it is legal. The government hence realizes a double benefit: first it collects new taxes, and second it spends less on repression because mafia organisations are weakened by the legalisation of their business.
Despite the controversy, legalisation has not yet been analysed as a tool to eradicate the smuggling industry and its implications in terms of migration equilibrium have not been fully studied by scholars or policy makers. By legalisation we mean total elimination of the smuggling industry through selling visas and not the exceptional amnesties, which have been repeatedly granted in the past to illegal migrants living in European countries such as Spain, Greece or in the US and pose an obvious problem of time consistency and credibility of the state.\textsuperscript{5} Our goal is thus to develop a model of legalisation to assess its policy relevance. We analyse how a set of tools including the sale of visa and various repressive measures, can be used to fight against smugglers while possibly achieving pre-defined migration flow targets. We do not discuss the optimality of such targets, nor the restrictive migration policies adopted by most advanced economies or their lax enforcement (for an analysis of such issues see Facchini and Testa, 2010).

Our analysis shows that the sale of visas at smugglers’ price, or higher, will not be sufficient to eliminate smugglers, nor to improve the skill composition of migrants. Indeed prohibition creates a barrier to the entry of the market where it applies. Mafia organisations rely on this legal barrier, and on violence, to cartelize the industry. They are hence able to charge high prices. We may thus expect the operation of smugglers’ cartels not to affect all immigrants equally but to act as a positive selection on immigrants, with higher prices disproportionately reducing the flow of lower income immigrants.\textsuperscript{6} In this context the big markups imply that smugglers may respond to legalisation measures by lowering the price they propose to would-be migrants and still make a profit. Legalisation will hence increase the flows of migrants and worsen their skill composition.

To be more specific we model the migration market as follows. The demand comes from workers, who choose to work in the foreign country or in the origin

\textsuperscript{5}See Chau, 2001, Epstein and Weiss, 2001, Karlson et al., 2003, Solano, 2009 on the rationale and optimal design of amnesties. See Mas, 2009, on their questionable effectiveness at decreasing the number of illegal migrants.

\textsuperscript{6}Similar effects were reported by multiple contemporary accounts following the cartelization of the shipping industry at the turn from the 19th to the 20th century
country, weighing the benefits of higher wages in foreign countries against migration costs. Migration price is determined by smugglers who maximise their profits. Policies shape the market structure. They may reinforce the market power of the smugglers by increasing their costs to operate and hence their prices, or force them to propose lower prices to compete with the migration visas on sale. We will see that neither traditional repressive measures nor more "innovative" pricing tools through the sale of migration visas are satisfactory policies. The former help to control migration flows but, far from suppressing smugglers, they may even increase their market power and the price paid by the migrants for their service. The latter help to eradicate smugglers' activities at the cost of substantially increasing migration flows. The paper then explores how a combination of these measures may be effective at eradicating smugglers and controlling migration flows, without necessarily increasing the budget deficit. Finally, using our model and estimates from previous studies on Chinese migration to the US, we calibrate the price of visas, which would drive smugglers out of business. This price varies between around $18000 when the risk of deportation for illegal migrants is low (around 20%) and around $50000 in case of high risk (around 70%). This result illustrates the importance of combining repression and legalisation to control demand: with a high level of repression leading to high risk of deportation for illegal migrants it is easier for the government to apply a high price for the visas, which will eliminate smugglers. In practice repression can take different forms and target different groups: the smugglers, the illegal migrants or the firms which employ them. Our simulations show that to implement legalisation without increasing migration flows, a government would need to increase by more than three times the marginal costs for smugglers to operate compared to its level under the status-quo. Alternatively this would require increasing the probability of deportation or enforcing firms' controls to reduce migrants' expected earnings to around 40% those of workers with the same skills employed in the legal sector of the economy. Several reasons why effective combinations of pricing and repression instruments have not yet been implemented to eradicate human smuggling are
then discussed with the policy implications of the paper.

There is an expanding theoretical literature on illegal immigration control, following Ethier (1986). Epstein et al. (1999) take into account its dynamic aspects, as migrants who enter legally may subsequently move into the illegal sector in order to avoid deportation and Djajić (1999) investigates its counterproductive effects as migrants may move into new sectors and new areas, where new migration networks may form. In practice countries such as Israel, Cyprus and Lebanon have tried to regulate long distance migration through local agencies located in South East Asian countries such as Philippines and Sri Lanka. These legal intermediaries organise the shipment of cheap labour force to compensate for shortages in labour. As migrants under these schemes are obliged to return to their home country at the end of their contract, this is the source of another type of illegal migration from those overstaying illegally in the destination country (Djajić, 2011, Schiff, 2011).

However, none of the papers on illegal migration mentioned above takes into account the organisation of the supply side of the market by smugglers, which is the main focus of our paper and is an important determinant of long haul migration flows, as suggested by the historical evidence on shipment cartels. Similarly none of the papers on legalisation studies the possibility of using standard economic tools such as sale of visas to control migration flows and the impact of such legalisation on migration equilibrium. While focusing on this particular channel of illegal entry (i.e., through the services of smugglers) makes the originality of the paper, this also limits the interpretation of the policy implications. We may expect spill-over effects on other channels, if would-be migrants choose between different methods of entry, which are beyond the scope of this paper.

By studying the response by smugglers to policy measures, our paper is close in spirit to Friebel and Guriev (2006), who model how smugglers establish labour/debt contracts with poor migrants, which force them to repay their fee. In this context, they show that deportation and border control policies do not have the same effects on illegal migration: stricter deportation policies
may increase the flow of illegal immigrants and worsen the skill composition of immigrants while stricter border controls decrease overall immigration and may result in an increase in debt-financed migration. A key assumption of their model is that migrants are liquidity constrained and cannot pay upfront the fee, which gives rise to these contracts.\footnote{Migrants may also respond to these debt labour contracts by choosing optimally the duration of repayment period and consumption behaviour and this affects the complementarities between border controls, deportation measures and employer sanctions as studied by Djajić and Vinogradova, 2011.} In a different context where contracts are not legally enforceable between traffickers and smuggled migrants, which leads to migrants’ exploitation, Tamura (2010) shows that destination countries with limited resources may prefer to improve the apprehension of smugglers and their clients at the border rather than inland.

In contrast to these papers we do not focus on liquidity constrained or on exploited smuggled migrants but on all workers who use the services of smugglers to migrate illegally\footnote{Note that financial constraints are likely to be less binding with the introduction of visas as migrants can more easily get a regular loan. And legalisation diminishes the scope for human trafficking as laws can be more easily enforced against exploitative smugglers.} and we study the effects of a larger set of policy measures - sale of visas versus more traditional repressive policies through border enforcement, deportation or employers’ sanctions - on the equilibrium of the market for smuggled migrants. Our results show that only a combination of them may be effective at both eliminating smugglers’ businesses and controlling migration flows, while limiting increases in budget deficit entailed by stricter controls. These results are robust to the introduction of risk, which, with the noticeable exceptions of Woodland and Yoshida (2006) and Vinogradova (2010), has rarely been addressed in previous studies on illegal immigration control.

The rest of the paper is organised as follows. Section 2 presents the set-up of the model and describes the market structure for illegal migration under status quo (absence of legalisation). Section 3 studies the effects of introducing pricing tools and repressive measures to regulate migration flows. Section 4 extends our model by taking into account the strong uncertainty that represents illegal migration for risk averse individuals. Section 5 uses calibrations to illustrate
the policy implications of the model and Section 6 concludes.

2 Migration equilibrium

This section studies the migration market equilibrium, when workers pay a migration price to the smugglers, \( p \), to migrate illegally to a high wages destination country. We thereby assume that individuals need to hire a smuggler if they wish to migrate.\(^9\) For simplicity of exposition, the analysis is first derived under the assumption that illegal migration entails no risk or equivalently that individuals are risk neutral. Section 4 shows that our results are robust to the introduction of risk aversion.

2.1 Demand for illegal migration

At the beginning of her working life of total duration 1, a worker maximises her lifetime utility. With perfect foresight she chooses her location either abroad or in her home country and consumes all her income.\(^10\)

Workers are heterogeneous according to their labour efficiency (or skill), \( \theta \), which is distributed identically and independently according to the density function \( f(\theta) \) and distribution \( F(\theta) \) over \([\bar{\theta}, \theta]\) with \( \bar{\theta} > 0 \).\(^11\)

If there is no migration visa for sale, we assume that workers can only work in the illegal sector of the economy such that expected earnings abroad are \( d \theta w_f \), with \( \theta w_f \) being the wages in the legal sector and \( d < 1 \). The discount factor \( d \) simply captures the fact that workers would have more opportunities if they worked legally rather than illegally.\(^12\) We assume for the moment that \( d \)

\(^9\) Although figures vary a lot across destination countries, we expect this to be the case where it is difficult to migrate through different channels, in particular when migration policies are very restrictive and when geographical borders do not exist between origin and destination countries. In the UK for example smugglers are involved in around 75% of detected cases of illegal border crossing (IND, 2001).

\(^10\) As there is no sequential decision-making the model is essentially static.

\(^11\) Instead of considering skill heterogeneity, we could easily embed into the model other dimensions of heterogeneity, which may affect the returns to migration (such as physical abilities or degrees of risk aversion in the extended model with risk outlined below) without changing its main results.

\(^12\) It is for example the case if they cannot easily change employer in the illegal sector or if they are caught in a debt-labour contract upon arrival (see Friebel and Guriev, 2006).
is exogenous but we will relax this assumption later on, in line with empirical evidence (Cobb-Clark et al., 1995).

Note that the way we model the returns to skills leads to a positive selection of illegal migrants. Indeed long distance illegal migration flows, which are difficult to undertake without the help of smugglers, are very costly for workers from low wages countries and this is likely to lead to a more positive selection of workers than that which has been documented for the Mexican migration.\textsuperscript{13} This also turned out to be the case in the High-Costs migration period after 1993 for Mexican workers, who were more severely liquidity constrained (Borger, 2011).\textsuperscript{14}

The worker knows the discounted income she will earn in the foreign country on the illegal market, $d w_f$, which is assumed higher than the discounted income in home country $w_h$:

$$d w_f > w_h$$

Note also that the labour market is considered exogenous, which is justified by the fact that the number of workers on the labour market is very large as compared to the flows of migrants. If she lives abroad earnings are used to consume and to pay for migration price $p$, such that she consumes $\theta d w_f - p$ whereas, if she stays in origin country, she consumes $\theta w_h$.\textsuperscript{15} Therefore the worker decides to migrate if her life time utility, equal to $u(\theta d w_f - p)$ in case she migrates, is higher than her utility in case she does not migrate, equal to $u(\theta w_h)$. With increasing utility functions, the migration condition can be rewritten as

\textsuperscript{13}As Hatton and Williamson put it (2008) "Greater distances, [...] and (for the poorest regions) the poverty constraint all imply that US and EU migrants coming from farther away should be more positively selected". However, most of the empirical evidence we have on selection is either on legal migration (see Beine et al, 2007 or Docquier and Rapoport, 2007) or on cross-border illegal migration between Mexico and the US such that it is difficult to validate this assumption empirically.

\textsuperscript{14}Although we present the model in the case of positive selection, it can easily be extended to the case of negative selection or intermediate selection as shown in the Appendix (8.1). In these cases, the key insights of the model would be very similar provided that the sale of visas is carefully designed and targeted to low-skilled workers in order to be effective at eradicating the smuggling industry.

\textsuperscript{15}She perfectly knows the wages per unit of time that she will get at home and abroad and the discount rate. She computes the net present value of her future flow of income. Since wages and discount rate are exogenous we avoid introducing separate notation and directly focus on net present values.
$\theta w_h < \theta dw_f - p$. This shows that individuals are more likely to migrate the higher the wage differential between foreign and home countries, the higher their skill level (what we called "positive selection") and the lower the migration costs.

Solving for the skill level such that an individual is indifferent between migrating illegally or not, we obtain the illegal migration threshold $\theta^I$ written as:

$$\theta^I = \frac{p}{dw_f - wh}$$

(1)

And aggregating over the distribution of skills, we obtain the demand for illegal migration as a function of migration price $p$:

$$D^I(p) = \int_{\theta} f(\theta) d\theta = 1 - F(\theta^I)$$

(2)

As $\theta^I$ increases with $p$ and decreases with $d$, the demand for migration is higher the lower the migration price, $p$, and the higher the wages differential $dw_f - wh$ between the two countries.

### 2.2 Supply of services

Because legal restrictions constitute barriers to market entry, the smuggling business is concentrated. A few criminal networks actually provide the service. We model the oligopolistic market for illegal migration as a generalized Cournot competition. We focus on symmetric equilibrium (i.e., each smuggler has the same market share). The detail of the computation is in Appendix 8.2. The generalized Cournot price with $N$ smugglers, $p^N$, is such that:

$$\frac{p^N - c}{p^N} = \frac{1}{N} \frac{1}{\varepsilon_{D^I,p}}$$

(3)

It is easy to check that when there is only one smuggler, $N = 1$, we are back to the standard monopoly case $p^1 = p^m$: the Lerner index is equated to the inverse of the price elasticity of demand. When on the contrary $N \rightarrow \infty$ we obtain the competitive case so that $p^\infty = c$. The generalized Cournot competition demand is between these two extreme cases: $D^I(p^m) < D^I(p^N) < D^I(c)$ for all $N > 1$. 

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For instance in the case of a uniform distribution of skills over \([0, 1]\), the following easily tractable closed form solution is derived (see Appendix 8.2):

\[
p^N = \frac{dw_f - w_h + Nc}{N + 1}
\]  
(4)

and the demand

\[
D^I(p^N) = \frac{N}{N + 1} \left(1 - \frac{c}{dw_f - w_h}\right)
\]  
(5)

is between the demand on a monopolistic market \(D^I(p^m) = \frac{1}{2} - \frac{c}{2(2w_f - w_h)}\), and the demand in perfect competition \(D^I(c) = 2D^I(p^m)\).

The analysis of smugglers pricing behavior outlines that repressive policy measures may have very different effects depending on whether they directly affect the smuggling business or the demand for their services: any measure which increases the marginal costs for smugglers to operate, \(c\), such as increased border enforcement, will necessarily increase the fees paid by would be migrants, and, hence the abusive power of smugglers. In contrast, measures which decrease the discount factor to work in illegal sector, \(d\), such as sanctions to employers of illegal workers that are transmitted into lower wages paid to illegal migrants, decrease the fees charged by smugglers as they increase the demand elasticity.

In a more dynamic perspective, one could easily endogenise \(N\), the number of smugglers on the market. Denoting \(K\) the level of sunk costs to enter this market, the number of smugglers \(N\) is the integer part of \(\mu\) such that \(\pi(\mu) = K\) where \(\pi(\mu) = (p^\mu - c)D^I(p^\mu)/\mu\) is the firm rent. Therefore any repressive measure increasing \(c\) or \(K\) reduces the number of smugglers on the market, thereby increasing the price they charge for their services and lowering the demand for illegal migration.

It is also worth noting that the smugglers might face different populations of migrants. For instance, illiterate candidate from rural areas are different from educated workers from urban centers. If the oligopolistic smugglers can identify them, they will apply different prices to these different populations. As is standard with third degree price discrimination, groups endowed with the largest price elasticity will get the smallest price. In contrast captive migrants
(i.e., groups with low price elasticity) face higher prices.\footnote{Assume that they are $J$ different pools of migrants identified by $j = 1, \ldots, J$. The skill parameter of workers in group $j$ are distributed identically and independently according to the density function $f_j(\theta)$ and distribution $F_j(\theta)$ over $[\underline{\theta}_j, \overline{\theta}_j]$. Their wages might also be type dependent: $\{w_{f_j}, w_{h_j}\}$. The demand for migration in group $j$ is $D_j^L(p) = \int_{\theta_j^L(p)}^{\overline{\theta}_j} f_j(\theta) d\theta = 1 - F_j(\theta_j^I(p))$, where $\theta_j^I(p) = \frac{p}{w_{f_j} - w_{h_j}}$. The optimal smuggler prices determined by (3) vary from one group to the other according to the price elasticity of its demand $\varepsilon_{D_j^L(p)} = -\frac{p D_j^L'(p)}{D_j^L(p)}$.}

\section{Sale of visas}

This section studies the effects of selling migration visas when the smugglers have already paid for the fixed costs of smuggling. In order to eradicate smugglers the government might try to legalize the market for migration. To do so, it can create a permit to migrate that people can buy. A simple idea would be to create a permit that will cost the same price, $p^L$, as the price imposed by the smugglers to illegal migrants, noted $p^I : p^L = p^I$. However, this policy will increase migration flows. Comparing the legal migration threshold, written as $\theta^L = \frac{p}{w_f - w_h}$, with (1), it is easy to see that, for any given migration price $p$, the legal migration threshold is always lower than the illegal one: $\theta^L(p) \leq \theta^I(p) \forall p > 0$. This is because migration pay-offs are higher under legal than illegal migration, which increases the wages differential between foreign and home countries. More importantly such a pricing policy of legal migration will not eradicate smuggling.

To determine the pricing scheme for legal migrants a government, which is a Stackelberg leader,\footnote{This is the natural assumption as, once the government announces its policy, it must stick to it to be credible.} needs to take into account that the smugglers will react to its policy. The model is thus solved by backwards induction.

\subsection{Smugglers’ reaction to legalisation}

By comparing the payoffs if an individual of type $\theta$ migrates legally, $\theta w_f - p^L$, with the payoffs if she migrates illegally, $d\theta w_f - p^I$, we can determine the...
threshold type, $\theta^L$, defined as:

$$\theta^L = \frac{p^L - p^I}{(1 - d)w_f}$$

(6)

such that any individual above this threshold prefers to migrate legally than illegally. We can easily check that $\partial \theta^L / \partial d < 0$. This simply says that the larger the income differential between the legal and illegal sectors, the more individuals prefer to migrate legally than illegally.

Using (1), we can write the threshold type $\theta^I = \frac{p^I}{d_\theta^I - w_h}$ above which an individual prefers to migrate illegally through the smugglers than to stay in her origin country. If $\theta^L < \theta^I$ nobody chooses to migrate illegally. A constraint for the smugglers is to fix their price low enough as compared to the price of a legal permit in order to attract the workers of type between $\theta^I$ and $\theta^L$.

This constraint can be written as:

$$p^I < \frac{d_\theta^I - w_h}{w_f - w_h}p^L$$

(7)

This shows that the lower the relative payoffs of illegal migration as compared to legal migration, captured by the ratio $\frac{d_\theta^I - w_h}{w_f - w_h}$, and the lower the legal price of migration, $p^L$, the more difficult it is for the smugglers to satisfy this constraint.

Under this constraint, the demand faced by the smugglers is:

$$D^I(p^I, p^L) = \int_{\frac{p^I}{(1 - d)w_f}}^{\frac{p^L - p^I}{(1 - d)w_f}} f(\theta)d\theta.$$  

(8)

Let $p^N(p^L)$ be the solution of (3) computed with the direct price elasticity of demand (8), $\varepsilon_{D^I, p^I} = -\frac{\partial D^I(p^I, p^L)}{\partial p^I} \frac{p^I}{D^I(p^I, p^L)}$, which is parameterized by $p^L$. The price reaction function of the smugglers is the solution of the following equation:

$$p^I(p^L) = \begin{cases} p^N(p^L) & \text{if } p^N(p^L) < \frac{d_\theta^I - w_h}{w_f - w_h}p^L \\ 0 & \text{otherwise} \end{cases}$$

(9)

In the uniform example, we obtain a closed form solution (all mathematical proofs are derived in Appendix 8.4):

$$p^N(p^L) = \frac{N + 1}{w_f - w_h} \frac{d_\theta^I - w_h}{w_f - w_h} + \frac{N}{N + 1} c$$

(10)
The smugglers are active and apply this price if condition (7) holds, which is equivalent to:
\[ c < \frac{dw_f - w_h}{w_f - w_h} p^L \]

3.2 Government policies

Illegal activities linked to human smuggling entail large negative externalities for societies. In Mexico for example, human smuggling is often integrated with the drug business and other criminal activities, which lead to high insecurity and became recently one of the main electoral concerns.\(^\text{18}\) This is also true for OECD countries, where governments expend considerable resources in an attempt to eradicate this industry. For example, Sweden and Australia have recently adopted strict policies against such criminal networks.\(^\text{19}\) This Section studies how economic tools can be used to reach this objective and their effects on the migration market.

3.2.1 Eliminating smugglers

We first consider a policy, which aims at breaking all incentives to smuggle. It consists in applying a low enough price for legal migration such that the smugglers will have negative profits. This requires that the marginal costs to smuggle are higher than the reaction price, i.e. \( p^I(p^L) \leq c \).

The threshold price, noted \( p^L \), below which the smugglers exit the market is such that \( \theta^L = \theta^I \) defined respectively in equations (6) and (1) for \( p^I = c \). That is, \( p^L \) is such that:
\[
\frac{p^L - c}{(1-a)w_f} = \frac{c}{aw_f - w_h}.
\]
This yields:
\[
p^L = \frac{w_f - w_h}{dw_f - w_h} c
\]


\(^\text{19}\)In its budget 2011-2012 the Australian Government has for instance specifically earmarked "$292 million to support a new Regional Cooperation Framework that will help put people smugglers out of business and prevent asylum seekers making the dangerous journey to Australia by boat." See the Webpage of the Australian Government: http://www.ag.gov.au/Publications/Budgets/Budget2011/Mediareleases/Pages/Strengtheningourbordersthroughregionalcooperation.aspx
In other words, the government that wants to push smugglers’ reaction price down until their mark-up vanishes has to apply the price $p_L$. Note that this result applies to any initial structure of the market for smugglers: monopolist, oligopolistic or competitive: irrespective of the initial market conditions, if the government wants to eradicate smugglers through legalisation it has to apply $p_L$ such that the smugglers end up reaching their marginal costs pricing.

Comparing $p_L = \frac{w_f - w_h}{dw_f - w_h} c$ and $p^{pc} = c$ we can establish, since $d < 1$, that the price imposed by the government to eliminate the smugglers is higher than the price imposed by smugglers under perfect competition. Nevertheless, the migration demand, which is now legal, can be written as:

$$D^L(p^L) = \int \frac{\theta}{c \frac{w_f - w_h}{dw_f - w_h}} f(\theta) d\theta$$

$$D^L(p^L) = 1 - F \left( \frac{c}{dw_f - w_h} \right)$$

This demand is exactly the same as the demand for illegal migration under perfect competition of smugglers: $D^L(p^L) = D^I(c)$. This is because, for a given migration price, more workers are willing to migrate legally than illegally. This result, which is robust to the introduction of risk aversion, is summarized in the next proposition.

**Proposition 1** A policy that reduces the number of illegal migrants to zero through the sale of visas yields the same level of migration as under perfect competition among smugglers.

It is not possible to empirically test the predictions of Proposition 1 since no country has, so far, used such a pricing scheme to eradicate human smuggling. However, the theoretical framework, which is quite general, applies to other markets with positive demand and legal prohibition. The theory predicts that destroying a mafia organisation by legalizing its activity will inevitably increase the demand of the formerly prohibited product or service. It is thus
useful to look at other products and services, such as alcohol, drugs or sexual services, that are, or have been, successively prohibited and legalised to assess the relevance of Proposition 1.

The main problem to test the impact of prohibition on consumption is the lack of data on trade volume during prohibition time. However, using mortality, mental health and crime statistics, Miron and Zwiebel (1991) estimate the consumption of alcohol during Prohibition in the US (1920-1933). They find that alcohol consumption fell sharply at the beginning of Prohibition, to approximately 30% of its pre-Prohibition level. During the next several years alcohol consumption increased, but remained below its pre-Prohibition level, at about 60-70%. Consumption increased to approximately its pre-Prohibition level only during the decade after Prohibition was abolished.

Another piece of evidence concerns prices. The theory predicts a sharp decrease in prices if one aims at eliminating mafia through legalisation. In line with this, Miron (2003) shows that cocaine and heroin are substantially more expensive than they would be in a legalized market: "the data imply that cocaine is four times as expensive as it would be in a legal market, and heroin perhaps nineteen times."

Finally, regarding the sex market, Poulin (2005) claims that the legalisation of prostitution in countries such as the Netherland, Germany or Australia, has generated an expansion of this industry: "An "abolitionist" country like France, with a population estimated at 61 million, has half as many prostituted people on its territory as does a small country like the Netherlands (16 million) and 20 times fewer than a country like Germany, with a population of around 82.4 million."

It is clear that more empirical studies are called to understand the consequences of legalisation. Yet, based on the theory and on the available empirical evidence, we predict a sharp increase in migration flows if visas were sold at the price that would drive the smugglers out of business.\textsuperscript{20} Dismantling the smugg-\textsuperscript{20}The higher the initial concentration of the market the larger the increase in flows following legalisation.
glers by lowering the price reduces the number of illegal migrants to zero by destroying smuggler profits, which is its primary objective, but it also increases migration flows and worsens their skill composition.

3.2.2 The policy trade-off: controlling migration flows

Such increases may not be acceptable in most OECD countries, where there is a strong popular demand for controlling migration flows. As we mentioned earlier we do not discuss here the optimality of such an objective but simply analyse whether standard economic instruments can help to reach it. We thus study what happens if the government sells visas to control migration flows. A constraint for the government is that the price of these visas, \( p^L \), has to be lower than \( p_L \), the threshold price above which no worker will migrate legally. This threshold is the minimum value of two constraints:

- The (IR) constraint: \( p^L \leq \overline{\theta}(w_f - w_h) \), which implies that someone at least prefers to migrate legally than stay at home, and

- The (IC) constraint: \( p^L \leq \overline{\theta}(1 - d)w_f + p^I \), which implies that someone at least prefers to migrate legally than illegally.

The legal migration is positive if and only if \( p^L \leq \min \{ \overline{\theta}(w_f - w_h), \overline{\theta}(1 - d)w_f + p^I \} \). Since by assumption 1, \( dw_f > w_h \) it is easy to check that the (IC) constraint is binding whenever the smugglers are active. Indeed \( \overline{\theta}(w_f - w_h) > \overline{\theta}(1 - d)w_f + p^I \) is equivalent to \( p^I < \overline{\theta}(dw_f - w_h) \), which, by virtue of (1), necessarily holds when the smugglers are active. We deduce that \( p^L = \overline{\theta}(1 - d)w_f + p^I \). Since the smugglers price, \( p^I(p^L) \), is endogenously determined in equation (9), the threshold \( p^L \) is a fixed point such that:

\[
p^L = \overline{\theta}(1 - d)w_f + p^I(p^L) \tag{13}
\]

Under the assumption that \( \frac{\partial^2 p^I(p^L)}{\partial p^L \partial p^I} \geq 0 \), which for instance holds with a uniform distribution of skills, one can check that \( \frac{dp^I(p^L)}{dp^L} \geq 0 \) (see Appendix 8.3). This implies that \( p^L \) exists and is unique. Indeed if \( p^L = 0 \) then \( \overline{\theta}(1 -
\( d w_f + p^I(0) > 0 \), while \( \bar{\theta}(1 - d)w_f + p^I(\infty) = \bar{\theta}(1 - d)w_f + p^N < +\infty \) where \( p^N \) is defined in equation (3). We deduce that \( p^L \) and \( \bar{\theta}(1 - d)w_f + p^I(p_L) \) cross once and only once at \( p^L > 0 \). It is worth noting that, contrary to \( p^L \) which is invariant, \( p^L \) depends on \( N \) the number of smugglers active in the market.\(^{21}\)

We want to study the objective function of a government that would aim at minimizing the increase in migration flows following the introduction of sale of visas. Since the status quo level of immigration is independent of the new policy to sell visas, this objective is equivalent to minimizing migration flows following this scheme. By using (1) the objective function is:

\[
\min_{p^L \leq p^I} \int_{\frac{p^I(p^L)}{d w_f - w_h}}^{\bar{\theta}} f(\theta) d\theta = \min_{p^L \leq p^I} \left[ 1 - F \left( \frac{p^I(p^L)}{d w_f - w_h} \right) \right]
\]

where the government internalizes the reaction function of the smuggler \( p^I(p^L) \) in (9). Since \( \frac{dp^I(p^L)}{dp^L} > 0 \) differentiating equation (14) with respect to \( p^L \) yields

\[
- \frac{1}{d w_f - w_h} f \left( \frac{p^I(p^L)}{d w_f - w_h} \right) \frac{dp^I(p^L)}{dp^L} \leq 0.
\]

A government, which aims at minimizing migration flows, will fix the highest possible price for its visas \( p^L \).

The migration demand under such policy is higher than in the case of an unconstrained smuggler oligopoly. Indeed when \( p^L \leq p^L \leq \bar{\theta}(w_f - w_h) \), the smugglers are the only ones to be active on the market as nobody wants to migrate legally if the smugglers apply their optimal reaction price \( p^I(p^L) \). However they cannot apply the unconstrained oligopoly price \( p^N \) of equation (3) as some migrants would then choose legal migration, lowering the smugglers’ profit. This entails larger migration flows even though no visa is sold in such case.\(^{22}\)

Figure 1 illustrates this result in the uniform example. It shows the reaction function \( p^I(p^L) \) as defined by (10) where the non-zero part of the reaction function, \( p^N(p^L) = \frac{p^L}{N+1} \frac{d w_f - w_h}{w_f - w_h} + \frac{N}{N+1} c \), decreases with \( N \geq 1 \). It becomes flat

\(^{21}\)This result illustrated below in the uniform distribution example is intuitive: the upper limit for visa prices decreases with the number of smugglers on the market since their response price decreases with the degree of competition and the government has to compete with them to encourage legal migration.

\(^{22}\)Smugglers are unconstrained to apply their oligopolistic price only when \( p^L > \bar{\theta}(w_f - w_h) \).
when $N$ goes to infinity (i.e. it converges to the constant value of $c$). \(^{23}\)

The next proposition, which is robust to the introduction of risk-aversion, summarizes the policy result this section implies:

**Proposition 2** Regulating migration flows through the sale of migration visas necessarily increases the total number of migrants and lowers their average skill level.

Proposition 2 implies that a government that aims at minimizing the demand for migration, cannot do better than an unconstrained monopoly smuggler. So, if the objective is to decrease the total number of migrants, there are more effective policies than selling migration visas. Using our results above it is straightforward to check that any instrument that increases the concentration of smugglers on the market through the entry sunk cost, increases their costs to operate, $c$, or decreases the benefits of illegal migration, $d$, is more effective at controlling migration demand.

So far we have considered two types of policies: one policy relies on pricing schemes and economic tools to eliminate smuggling, while the other policy is essentially repressive and aims at controlling illegal migration flows. Both solutions are politically unsatisfactory. The former leads to a substantial increase in migration flows, while the latter does not eradicate smugglers and increase their market power (i.e., market concentration). In what follows we explore how a combination of both types of approaches might help to simultaneously fight the smugglers and control migration flows, without increasing the burden of public deficit.

### 3.2.3 Affordable migration control through legalisation

In this section we consider a policy where the funds raised from the sale of the legal permits are used to fight illegal migration by increasing $c$ and decreasing

\(^{23}\)With the uniform distribution example, replacing (10) into (13) the upper limit for the visa price satisfies: $p^L = \left[ Nc + (1 + N)(1 - d)w_f \right] \frac{w_f - w_h}{(1 - d)w_f + N(w_f - w_h)}$. Comparing the reaction smugglers price $p^I(p^L)$ with the unconstrained smugglers’ oligopoly price $p^N$ defined in (3) it is straightforward to check that $p^I(p^L) \leq p^N$ if and only if $dw_f - w_h \geq c$, which is the necessary condition for the smugglers being active in the first place (see the Appendix 8.4).
d in such a way that increases in migration flows following the legalisation are limited as much as is affordable.

We start from the status quo situation where the marginal cost to smuggle is c and the discount rate to work as an illegal workers is d. The government can use a share of the new funds raised through the sale of migration permits to increase the smugglers’ marginal costs by reinforcing "external" (or border) controls. We denote \( c(R_1) \) the marginal costs that the smugglers face when the government invests \( R_1 \geq 0 \) in additional repression. We assume that, in the absence of additional investment, the marginal costs of the smuggler are the status quo level: \( c(0) = c \). Moreover we assume that \( c'(R_1) > 0 \) and \( c''(R_1) < 0 \). The concave shape indicates decreasing returns to scale in the fight against smugglers.

Similarly, the government can use another share of the funds raised through the sale of visas to increase "internal" controls at worksites and enforce the sanctions paid by the employers of illegal migrants. We denote \( d(R_2) \) the illegal migrant wage discount factor resulting from increased enforcement measures. Here again we assume that, in the absence of additional investment \( d(0) = d \), and that \( d'(R_2) < 0 \)\(^{24}\) and \( d''(R_2) > 0 \). The convex shape indicates decreasing returns to scale in the fight against illegal employment.

Replacing c by \( c(R_1) \) and d by \( d(R_2) \) in (11), we can determine the new legal migration price such that smugglers do not have any interest to operate given their inflated marginal costs and reduced migrant wages:

\[
\pL(R_1, R_2) = \frac{w_f - w_h}{d(R_2)w_f - w_h}c(R_1)
\]  

We deduce that the increase in demand following the introduction of the sale of visas for legal migration would be defined in (12) with the price \( \pL \) being replaced by \( \pL(R_1, R_2) \):

\[
D^L(R_1, R_2) = 1 - F \left( \frac{c(R_1)}{d(R_2)w_f - w_h} \right)
\]  

\(^{24}\)See Woodland and Yoshida, 2006, for a theoretical foundation of this assumption and Cobb-Clark et al. (1995) for empirical evidence.
Finally, the government chooses the investments $R_1$ and $R_2$ so as to minimize the increase in migration flows following the introduction of visas, under the constraint that the cost of repression is covered by the visa sales:

$$\min_{R_1, R_2} D^L(R_1, R_2) \quad \text{s.t.} \quad R_1 + R_2 \leq D^L(R_1, R_2)p^L(R_1, R_2). \quad (17)$$

Focusing on interior solutions the optimal affordable policy, which is derived in Appendix 8.5, is summarized in the next proposition.\textsuperscript{25}

**Proposition 3** A government that aims at dismantling smugglers while limiting migration flows without increasing its budget deficit invests the amounts $(R_1^*, R_2^*)$ solution of the following equations:

$$R_1 + R_2 = p^L(R_1, R_2)D^L(R_1, R_2) \quad (18)$$
$$\frac{c'(R_1)}{c(R_1)} = \frac{-d'(R_2)w_f}{d(R_2)w_f - w_h} \quad (19)$$

Equation (18) shows that the government invests the maximum possible amount in re-enforcing border controls and employers’ sanctions, which is affordable through the sale of visas. The optimal allocation of the budget for repression is such that the marginal impact of $R_1$ on $D^L$ is equal to the marginal impact of $R_2$ on $D^L$, as shown by (19). Note that enforcing the fines paid by employers of undocumented workers may contribute to raising additional funds for the government, which could easily be embedded into our model by adding a term (increasing with $R_2$) on the right hand side of the budget constraint in (17). The optimal investments $R_1$ and $R_2$ would be changed accordingly.

Since the demand for visas is a normal good and since $c'(R_1) > 0$ (alternatively $d'(R_2) < 0$) it is straightforward to check that $\frac{dD^L(R_1, R_2)}{dR_1} < 0$ (and that $\frac{dD^L(R_1, R_2)}{dR_2} < 0$). When repression against smugglers increases, the marginal cost of their activity, $c$, increases, which is transmitted to the smugglers’ price. Similarly, when sanctions are enforced against employers of illegal migrants, this is transmitted to the payoffs of migrants through a decrease in $d$. As a result

\textsuperscript{25}Depending on the functions $c(.)$ and $d(.)$ it may be the case that the optimal solution involves repression to increase $c$ only (i.e., $R_2 = 0$) or to decrease $d$ only (i.e., $R_1 = 0$). However, in other cases there will be an interior solution defined in (19).
the government can raise the price of legal visas without fuelling smugglers’ demand. This policy enables the government to control migration flows without relying on the help of smugglers. Indeed, by construction, such policy pushes smugglers out of the market by eroding their profits.

4 Risk aversion

So far we considered either situations entailing no risk or risk neutral individuals. It is probably more realistic to consider that individuals are risk averse. As migrating illegally entails important risks, this may be of significance to determine the number and type of migrants. This section shows the robustness of our results to the introduction of risk aversion. It reports only the main results. For the detailed computations we refer to Appendix 8.6.

We extend the model by introducing standard CARA utility function 
\[ u(x) = \frac{1}{a} \exp(-ax), \]
where \( a \) is the absolute risk aversion parameter. We also assume that illegal migration entails a risk: once the migrants pay the sunk costs to the smugglers and reach the destination country, they may stay abroad with probability \( 1 - q \), but have a probability \( q \) of being deported and sent back to their home country. In order to compare the results in the cases with and without risk aversion, we assume that if they manage to avoid deportation while in migration, they earn a wage \( \delta w_f \) with \( \delta \leq 1 \) so that the expected revenue from illegal migration is the same in the two cases, which can be written as:

\[ (1 - q)\delta w_f + qw_h = dw_f \]

Any distortion can hence be ascribed to the introduction of the risk aversion.

One can check in Appendix 8.6 that the illegal migration threshold \( \theta_{\text{ra}} \) is now a solution of the following equation:

\[ \frac{1 - e^{-ap'}}{1 - e^{-a(\delta w_f - w_h)}} = 1 - q \]

The risk neutrality (and/or absence of risk) benchmark case of equation (1), \( \theta' = \frac{p'}{\delta w_f - w_h} \), is simply obtained in equation (21) by setting \( q = 0 \), which also
implies, according to (20), that \( \delta = d \). Since \( \theta_{\text{ra}}^{I} \) is increasing with \( q \) and since \( \theta_{\text{ra}}^{L} = \theta^{I} \) when \( q = 0 \) we deduce that \( \theta_{\text{ra}}^{I} > \theta^{I} \) for all \( q > 0 \). This shows that, as we may expect, the risk of being deported discourages risk averse individuals to migrate illegally.

The logic of the pricing scheme of smugglers described in section 2 remains the same as before but it takes into account the new (lower) demand from risk averse individuals. Risk aversion implies that the price imposed by smugglers is then lower than the price they would impose to risk neutral individuals with the same expected revenue from migration, an intuitive result formally shown in Appendix 8.6.

**Lemma 1** Risk aversion limits the number of illegal migrants, \( \theta_{\text{ra}}^{I} > \theta^{I} \), and reduces the price imposed by smugglers \( p_{\text{ra}}^{I} < p^{I} \).

We now turn to the government policy of visa sale and the reaction of smugglers. If individuals can buy a legal permit to migrate at price \( p^{L} \), smugglers need to price their services low enough so that at least one individual wishes to migrate illegally. The skill level \( \theta_{\text{ra}}^{L} \) of the migrant who is just indifferent between migrating illegally and legally satisfies the following equation:

\[
\frac{1 - e^{-a(\theta(w_f - w_h) + p^{L} - p^{I})}}{1 - e^{-a(\delta w_f - w_h)}} = 1 - q
\]

Solving for the threshold \( \theta_{\text{ra}}^{L} \) and comparing it to (6) we show in Appendix 8.6 that risk aversion increases the demand for legal visas as established by Lemma 2.

**Lemma 2** Risk aversion increases the demand for legal visas: \( \theta_{\text{ra}}^{L} < \theta^{L} \).

When legal visas are put on sale, risk averse individuals are willing to pay a higher price to get valid documentation. Since we also showed that \( \theta_{\text{ra}}^{I} > \theta^{I} \), risk aversion reduces the illegal migration demand, \( D_{\text{ra}}^{I}(p^{I}, p^{L}) = \int_{\theta_{\text{ra}}^{L}}^{\theta_{\text{ra}}^{I}} f(\theta) d\theta = F(\theta_{\text{ra}}^{L}) - F(\theta_{\text{ra}}^{I}) \), by the two ends. On the one hand, in the absence of legal pricing schemes, illegal migration flows are lower if individuals are risk averse.
than if they are risk neutral. On the other hand, selling visas decreases illegal migration flows even further since individuals are less willing to bear the risk of deportation.

For the sake of realism we focus on situations where smugglers are initially active in equilibrium. Their reaction function, \( p_{ra}^L(p^L) \), is the solution of the same equation as in (9) using the demand \( D_{ra}^I(p^I, p^L) \). If the government wants to eliminate them by its pricing policy, it still needs to push their reaction price to the limit value \( c \) so that \( \theta_{ra}^L(c, p_{ra}^L) = \theta_{ra}^I(c) \). It follows that Proposition 1 holds true under risk aversion.\(^{26}\) If the government wants to eradicate smugglers through legalisation it will face the same demand as under perfect competition among smugglers: \( D^L(p_{ra}^L) = D_{ra}^I(c) \). The main difference is that the demand is lower than in the risk neutral case, \( D_{ra}^I(c) < D^I(c) \).

We show in Appendix 8.6 that \( p_{ra}^L \) is increasing with \( q \). Moreover as for \( q = 1 \) \( p_{ra}^L = p^L \) this implies that the visa price, which drives smugglers out of business, is higher with risk (when \( q > 0 \)) than without as established by Lemma 3.

**Lemma 3** Risk aversion increases the visa price, which drives the smugglers out of business: \( p_{ra}^L > p^L \).

Finally the results of section 3.2.2 are robust to the introduction of risk aversion. If the smuggler is active the binding constraint is the IC and \( p_{ra}^L \) is the solution of the following equation derived in Appendix 8.6:

\[
e^{-a(r_{wa}-p^L)} = (1-q)e^{-a(r_{wa}-p_{ra}^I(p^L))} + qe^{-a(r_{wa}-p_{ra}^I(p^L))} \tag{23}
\]

Therefore the rest of the reasoning and Proposition 2 hold true.

Proposition 3 can also be generalized taking into account the risk entailed by migration. With risk averse migrants the government has more instruments to raise the visa price that drives the smugglers out of business and, hence, limit migration flows. By investing in repression it can, as before,\(^{26}\) We can also see that Proposition 1 does not depend on the specification of the Demand function. Hence it is robust to other specifications of utility functions.
increase marginal costs for smugglers to operate through the increasing concave function $c(R_1)$, or decrease the benefits of working as an illegal worker through the decreasing convex function $\delta(R_2)$. In addition, it can also increase the probability of deportation $q$ through the increasing concave function $q(R_3)$. This new instrument is relevant only under risk aversion. Let $p^L(R_1, R_2, R_3) = \frac{w_f-w_h}{\delta(R_2)w_f-w_h} \log \left( \frac{1-q(R_3)}{e^{-c(R_1)a}-q(R_3)} \right)$ be the price that eliminates human smuggling and let $D^L(R_1, R_2, R_3) = 1 - F \left( \frac{p^L(R_1, R_2, R_3)}{w_f-w_h} \right)$ be the legal demand for visas associated with this price. Focusing on interior solutions Proposition 4 summarises how these three instruments can be optimally combined.\cite{27}

**Proposition 4** A government that aims at dismantling smugglers while limiting migration flows without increasing its budget deficit invests the amounts $(R_1^*, R_2^*, R_3^*)$ solution of the following equations:

\begin{align}
R_1 + R_2 + R_3 &= D^L(R_1, R_2, R_3)p^L(R_1, R_2, R_3) \\
\frac{c'(R_1)a e^{-c(R_1)a}}{e^{-c(R_1)a}-q(R_3)} &= \frac{-\delta'(R_2)w_f}{\delta(R_2)w_f-w_h} \log \left( \frac{1-q(R_3)}{e^{-c(R_1)a}-q(R_3)} \right) \\
&= \frac{q'(R_3)}{1-q(R_3)} \frac{1 - e^{-c(R_1)a}}{e^{-c(R_1)a}-q(R_3)} \\
\end{align}

As shown by equation (24) the government invests the maximum possible amount in re-enforcing border controls, employers’ sanctions and deportations, which is affordable through the sale of visas. And the optimal allocation of repression between the various instruments is such that their marginal impact on the demand is equalized (i.e., $\frac{\partial D^L}{\partial R_1} = \frac{\partial D^L}{\partial R_2} = \frac{\partial D^L}{\partial R_3}$).

Moreover, we find that the investment to increase the probability of deportation, $R_3$, which minimizes migration flows is higher than the investment that would minimise expected income from illegal migration (see Appendix 8.6).

This result, in line with Becker 1968, simply states that since individuals are

\cite{27}Depending on the functions $c(\cdot), \delta(\cdot)$ and $q(\cdot)$ it may be the case that the optimal solution involves repression to increase $c$ only (i.e., $R_3 = 0$), to decrease $\delta$ only (i.e., $R_1 = R_3 = 0$), to increase $q$ only (i.e., $R_1 = R_2 = 0$), or any combination of two instruments only (i.e., $R_1 = 0$ or $R_2 = 0$ or $R_3 = 0$). However, in other cases there will be an interior solution defined in (25).
risk averse, they respond more strongly to a change in the probability of de-
portation, \( q \), than to a "compensated" change in their earning, \( \delta \), which would
leave equal their expected income of illegal migration.

The main issue raised by the policy of legalisation combined with tight mi-
gration control is its effectiveness at limiting migration flow without weighing
too much on public finances. This ultimately depends on the elasticities of the
functions \( c(R_1) \), \( \delta(R_2) \) and \( q(R_3) \). Policy makers have to take into account that
these elastics vary from one country to the other. For example, when there is
a physical border between two countries it is difficult to raise smugglers’ costs
by increasing repression, as the evidence on illegal migration between Mexico
and the US mentioned in the introduction shows. Hence, the elasticity of the
function \( c(R) \) is likely to be low. By contrast, in the case of long-haul migration,
it might be easier to increase smugglers’ costs by reinforcing external controls.

Similarly, in countries with a large informal sector, it will be harder to reduce
\( \delta \), than in countries with a small informal economy. With inelastic functions
\( c(R_1) \), \( \delta(R_2) \) and \( q(R_3) \), the equilibrium price of migration visas will be quite
low. Such a policy of legalisation will be ineffective at limiting migration flows,
unless investments into additional repression are extremely high. This poses
a policy trade-off: high burden on public finances or large increase in migra-
tion flows, which will be hard to sustain politically. Moreover, in practice, the
way the repressive policy is set up is very important. The goal is to raise the
smugglers’ costs to increase their concentration, and not necessarily to disman-
tle existing cartels. Breaking established smugglers networks might give rise,
through the emergence of several smaller smuggler networks, to more compe-
tition in the illegal migration business and, hence, to lower prices and higher
demand.\(^{28}\)

\(^{28}\)The failure of the "war on drugs" launched in the United States in the 1980s has been
partly explained by such effects. The US authorities decided to infiltrate the drug mafia to
dismantle it. The infiltration operation, which was very costly, was successful. The disman-
tling of the well organized cartels which followed gave rise to the emergence of many smaller
drug networks fighting fiercely in price to gain market share. As a result, the consumption of
cocaine increased in the US (see Poret 2002).
5 Policy Implications

As it is impossible to run regressions to test our model, this section uses calibrations to interpret its results and quantify the policy effects outlined above. While interpreting our results we have to keep in mind that they are not full-fledged policy simulations. The model focuses on the migration market only and abstracts from any other changes that may occur in the rest of the economy as a consequence of large increases in migration flows. In particular, adjustments on the labour market may dampen the initial incentives to migrate, leading to smaller increases in migration flows following sale of visas than the ones we calibrate. Also, this may generate complex politico-economic problems, as not everybody in the host country will have the same welfare gains or losses following these changes. These are not captured by our model and the implications we draw below are purely used to illustrate the partial equilibrium effects on the migration market outlined by our model.

We borrow most of the estimates used in our calibrations from Friebel and Guriev, 2006, and from the scarce information we have on the smuggling industry from case-studies on Chinese smugglers (Yun and Poisson, 2005). As there is very little quantitative information on the risk faced by illegal migrants and on the degree of concentration of the market of smugglers, we also analyse the sensitivity of our simulations when risk varies and when the number of smugglers varies.\footnote{For example Chin and Zhang, 2002, stress the existence of several smugglers operating in China.}

5.1 Price of visas and migration demand following the legalisation

This section estimates the increase in demand for illegal migration following a legalisation scheme that would keep constant the marginal costs for smugglers to operate, the sanctions against employers and the probability of deportation i.e. not using the other available instruments.

Before quantifying the policy implications of our model we check in Appendix
that the incentive rationality constraint of our model is satisfied for the wages differential observed between the US and China in 2005 as well as for a large range of wage differentials that have been reported between advanced and developing countries (Clemens et al., 2009).

For all our simulations detailed in the Appendix we need some estimate of the degree of risk aversion of would-be migrants, \( a \), and of the deportation probabilities \( q \), which are typically difficult to observe. Instead, we have some direct evidence from Chinese smugglers reporting their marginal costs to operate at around €8000 to cross the borders to France and higher to the US (Yun and Poisson, 2005), which we estimate to be around $10000 for our simulations. Using this information, the lower bound of the price paid by Chinese to migrate illegally to the US, \( p^I = $35000 \), and our model we can infer a range of risk parameters \( a \) compatible with a range of deportation probabilities, \( q \) (see Appendix (8.8)). To perform some static comparative on the effects of varying the risk we can vary \( q \) in the neighborhood of the chosen values \((a, q)\).

We first simulate the visa price that would eradicate the smugglers using equation (54). Row 3 of Table I shows that, for each degree of risk aversion \( a \) considered successively in columns (1) to (4), the price increases with risk, which we established theoretically by Lemma 3. In column (1) this price ranges between $43624 and $49954 for probabilities of deportation, \( q \), between 0.68 and 0.72. In column (4), the visa price ranges between $17755 and $18957 for probabilities of deportation between 0.18 and 0.22. Since the absolute risk aversion parameter \( a \) compatible with the different ranges of \( q \) decreases with the probability of deportation, we deduce that the visa price is very sensitive to the risk entailed by illegal migration. Indeed a relatively high \( a \) coupled with a low \( q \) leads to much smaller equilibrium visa prices than a relatively low \( a \) coupled with a high \( q \).

We then estimate the magnitude of the increase in demand resulting from

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30This is an average. Marginal costs vary depending on the type of trip undertaken and on the type of migrant. Some Chinese migrants obtain fake visas and invitations for business trips, which allow them to travel directly by air. Others have to cross several borders using several intermediary smugglers, which increases the overall marginal costs of the operation.
the sale of visas, \( \Delta D = \frac{D^L(p^L, q^L) - D^L(p^I)}{D^L(p^I)} \), which will of course depend on the distribution of migrants' skills. Assuming a uniform distribution, our simulations show that the relative increase in demand following legalisation increases in risk and varies between around 20% for low values \( q = 0.18 \) and 55% for high values \( q = 0.72 \), as displayed in Row 4 of the table.

Tables A1 and A2 in the Appendix reporting the simulations for \( N = 3 \) and \( N = 5 \) show that the more competitive the smugglers' market the smaller the increase \( \Delta D \). This is an intuitive result since strongly cartelised smugglers keep the demand for illegal migration at a low level with high prices charged to migrants. Accordingly our simulations assuming \( N = 2 \) give higher bounds for all implied changes.

### 5.2 Legalisation with migration control

The simulations above were made assuming that the level of repression is kept constant by the government. We now allow the government to combine legalisation with "repressive" instruments in order to control migration flows. Since we do not know the functions \( c(\cdot), q(\cdot) \) and \( \delta(\cdot) \) it is not possible to simulate the optimal combination of instruments, which would minimise the increase in demand following the affordable legalisation scheme described in Proposition 4. Instead, we take one given objective, "0 migration increase", and show how different repressive instruments may be combined with visa sales to reach it.

Policy makers may first consider re-inforcing border controls, which would increase marginal costs for smugglers to operate. Solving \( D^L(p^I) = D^L \left( \frac{c^L}{p^L} (R^*) \right) \) and replacing with (62) and (63) gives straightforwardly \( c(R^*) = p^I \). As \( c(\cdot) \) increases with \( R \), this determines a unique level of repression above which the policy of legalisation with repression brings a lower level of migration than under the status quo. To give an idea of the magnitude of the required efforts we can compare the level of marginal costs for smugglers to operate, which must be equal to $35000 following the policy, to the marginal costs for Chinese smugglers reported

\[ ^{31} \]We can also use the simulations to show that the compatible values of risk with \( N = 10 \) would imply that \( q \) is lower than 0.05, which makes this case not very plausible.
to be around $10000 under status quo. Therefore the policy would require increasing the marginal costs for smugglers by 250% (i.e. $\Delta c = \frac{c(R^*)-c}{c} = 2.5$ such that $c(R^*) = 3.5c$). As it seems reasonable to assume decreasing returns to scale for border enforcement measures this would require increasing by more than 3.5 times the budget allocated to such measures.

Our simulations using (65) also show also that the additional efforts required to reach the objective decrease with the probability of deportation.\(^{32}\) Indeed, when risk is low the differential between smugglers’ price and marginal costs is large. As already shown in Lemma 1, when risk increases smugglers have to lower their margin to be able to attract risk-averse migrants. It is therefore easier to drive them out of business and keep migration demand constant when the risk of deportation increases.

Policy makers could alternatively reinforce the sanctions to employers of undocumented employees, which would translate into lower expected earnings abroad for illegal migrants. With the same reasoning as above we determine the relative decrease in the discounting factor, $\Delta \delta$, which yields the same level of migration following legalisation as under the oligopolistic market for smugglers (status quo). Using equation (66) Row 6 of Table I shows that this policy would require decreasing the discount factor $\delta$ by around 50%, such that the earnings of workers employed in the illegal sector of the economy falls below 40% ($0.5 \times 0.8$) of those of same skill workers in the legal sector.

For each instrument considered successively we see that the level of additional investments in repression required decreases with the deportation risk entailed by illegal migration. Since the risk of deportation $q(R^*)$ can also be interpreted as a policy instrument, our results highlight strong complementarities between different types of repressive instruments. Tables A1 and A2 show the robustness of the results to $N = 3$ and $N = 5$ respectively.\(^{33}\)

\(^{32}\)Within each column of row 5 of Table I $\Delta c$ decreases as $q$ increases. Note that , by construction of the pairs $(a, q)$, each column is such that $\Delta c = 2.50$ for the central value of $q$ of the neighbourhood considered.

\(^{33}\)Comparing results of Table I with those in Tables A1 for $N = 3$ or A2 for $N = 5$ shows that the efforts required to eliminate the smugglers and maintain migration demand constant are smaller the higher the number of smugglers on the market, an intuitive result. It is indeed
5.3 Discussion

The previous section highlights the complementarity between the different repression instruments. The optimal combination depends on the elasticities of the functions $c(R_1)$, $\delta(R_2)$ and $q(R_3)$. Although we do not have precise estimates of these elasticities, it seems unlikely that the combination currently adopted by the US and most EU countries is optimal. There are huge discrepancies between the amounts invested in border control versus employer’s sanctions. For example, in 2008 in France, only 1706 labour inspectors were employed for more than 3.8 million firms. Among those firms, only 1.6 million, the largest ones, were eligible for a control although many illegal migrants work in small construction firms and in restaurants. At the same time France has spent hundreds of millions of euros on repression measures such as dismanteling illegal immigrants’ camps, police enforcement at the borders and deportation measures. Similarly in the US, there is very little enforcement against illegal immigration at workplaces (Hanson, 2007). Between 1999 and 2003, the number of man hours US immigration agents devoted to worksite inspections declined from 480,000 to 180,000 hours and few US employers who hire illegal immigrants are detected or prosecuted. But considerable amounts have been increasingly invested in the controls of the US borders. The number of man hours spent policing the US-Mexico border increased by 2.9 times between 1990 and 2005 and the Border Patrol, which was increased from 9,000 agents in 2001 to 20,000 in 2009, costs less difficult to fight against smugglers when their initial profit is low, which decreases with the level of competition.


35With only 22590 controls to check for illegal workers, an eligible firm is inspected on average once every 70 years, or alternatively faces a 1.42% probability of being inspected each year and smaller firms face a 0 probability of inspection.

36The number of US employers paying fines of at least $5,000 for hiring unauthorized workers was only fifteen in 1990, which fell to twelve in 1994 and to zero in 2004 (see ''Immigration Enforcement : Preliminary Observations on Employment Verification and Worksite Enforcement" GAO-05-822T June 21, 2005, cited by Hanson 2007, p19.)

37The Washington Post, July 18, 2010 reported that more than 670 miles of border fences, walls, bollards and spikes that Congress decreed in 2006 at an estimated cost of $4 billion (plus future maintenance) had been almost completed.
an estimated $4 billion annually. The evidence on illegal migration between Mexico and the US mentioned in the introduction shows that such a policy of external control is ineffective at limiting migration flows.

The effects of stricter internal repression measures, which would increase penalties paid by employers of undocumented immigrants and deportation probabilities (decreasing $\delta$ and increasing $q$), are even less known and studied than the effects of stricter external controls (increasing $c$). Yet such policies have proved to be effective, at least in other industries. Focusing on the sex business, Poulin (2005) shows that repressive policy can successfully decrease demand, when, as in Sweden, legislation is passed to prosecute the customers, who are the final users of the business. As technologies develop to detect forged documents, for example using biometric identity cards, prosecuting firms that employ illegal workers could be a much more cost effective way to legalise and control migration flows than border enforcement measures. Moreover fines paid by employers would contribute to raising additional funds to make the legalisation policy even more affordable. It is striking that despite several attempts to mandate participation by all U.S. employers in the E-Verify program, an Internet-based system designed to check the employment authorization status of employees, participation is still voluntary, with limited exceptions. Small businesses and agricultural employers are strongly opposed to mandatory E-Verify and actively lobby against it. The American Farm Bureau Foundation stated in July that it "could have a significant, negative impact on US farm production, threatening the livelihoods of many farmers and ranchers in labor intensive agriculture." Similarly, within the European Union, representatives of Business Europe are opposed to the Commission’s idea that employers should check the validity of residence permits and risk being excluded from public contracts and, under certain circumstances, penalised by temporary or permanent closure of their companies (Bertozzi, 2009).
6 Conclusion

This paper has addressed a simple question: is there a role for the state to regulate migration flows by selling visas to would-be migrants?

The answer is nuanced. When smugglers have already paid fixed costs to settle their businesses, it is difficult for the government to compete. The model shows that dismantling smugglers networks by proposing a low enough price would be at the cost of increasing substantially migration flows and decreasing the average skill level of migrants. Hence there is a trade-off between suppressing smugglers or having fewer migrants in the economy.

If the goal is to control migration, demand is the lowest with a monopolistic smuggler. Hence increasing cartelisation of the market and/or increasing repression contribute to controlling migration flows. However, such measures are not satisfactory either, as they increase the price paid by illegal migrants and, hence, increase the amount of resources feeding the illegal sector of the economy. The paper proposes instead to combine different types of repression measures with pricing tools to dismantle the smugglers while limiting migration flows. Simple calibrations show that the additional investments required to reach this objective strongly decrease with the degree of risk entailed by illegal migration. For probabilities of deportation between 20% and 70% the price of visas that permit evicting the smugglers, calibrated using rough estimates borrowed from the literature, ranges between $18,336 and $46,575, which would lead to an increase in migration demand between 24% and 49%. The paper hence illuminates the complementarity between repression and legalisation.

Finally, the question that remains largely open is why a policy mix using traditional instruments combined with pricing tools has not yet been implemented to eradicate the smuggling industry. Although answering this question is beyond the scope of the paper, we may consider a few hypotheses that are worth investigating in future work and other fields of social sciences. In countries like France one immediate answer is that the legal framework is very strong and could not easily be modified to introduce such pricing schemes, which, in
the field of migration, would be considered as unethical or violating human rights. From this viewpoint, it is not clear that transparent pricing tools would be less ethical than the existing policy of visa rationing, which creates "rents" to the lucky applicants, generates important monetary "hidden costs", such as briberies, paid by all applicants, and feeds all kinds of illegal activities.

A second answer suggested by our results is that "natives" may prefer to have fewer and lowly paid illegal immigrants rather than a larger number of legal workers, who would enjoy a more complete set of rights, including access to social benefits, public services and political rights. Moreover, given the discrepancies between the investments in external and internal controls, the debated effectiveness of border enforcement measures and the availability of new technologies, systematic controls of undocumented workers at the workplace is a much more promising means of controlling illegal migration than border enforcement. Accordingly, effective migration control should involve reinforcing sanctions paid by employers of illegal migrants. Although this may be a more cost-effective way to combine legalisation with migration control than reinforcing border controls, such policy will typically encounter strong resistance from powerful lobbies as observed for example in the EU and in the US. This also suggests that the status quo reflects complex political-economy issues with some people benefitting more than others from lax enforcement. All these considerations may explain why, under current policies, a large number of illegal migrants still bear the costs of being exploited in destination areas and face the constant risk of being deported.

Moreover people may not be willing to trade a sacred value such as the right to immigrate for money -what psychologist Philip Tetlock (2007) refers to as a "taboo tradeoff".

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38 Moreover people may not be willing to trade a sacred value such as the right to immigrate for money -what psychologist Philip Tetlock (2007) refers to as a "taboo tradeoff".
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8 Appendix

8.1 Negative or intermediate self-selection of illegal workers

In the presentation of our model we assumed that illegal workers self-select positively through migration according to their skill level. This generates interesting findings as a government will compete with smugglers to attract the highest skill workers of the poor economy by selling migration visas. However, depending on the relative returns to skill in the origin and destination countries the case of negative self-selection of workers (i.e. from the bottom of the skill distribution in the origin economy) through illegal migration cannot be ruled out, although we may argue that the high costs entailed by long distance migration may more likely yield positive selection. Moreover the existence of liquidity constraints may also generate an intermediate selection of illegal workers (i.e. from the middle of the skill distribution). These two types of selection characterise successively the large migration flows of undocumented Mexican workers to the US in the low costs period pre 1993 and high costs periods post 1993 as shown by Borger 2011.

To give the intuition of how the results would change in the case of negative selection, we will adopt the extreme assumption that workers working in the illegal sector of the destination country are paid at a flat rate, \(dw_f\) which does not depend on their skill.\(^{39}\) After writing the migration condition as \(w_h < dw_f - p\), we can solve for the skill threshold, noted \(\theta^I\), below which an individual prefers to migrate illegally than not to migrate:

\[
\theta^I = \frac{dw_f - p}{w_h}
\]

This shows that workers are more likely to migrate the higher the wage differential between foreign and home countries and the lower their productivity.

After aggregating over the distribution of skills, we obtain the demand for

\(^{39}\)Such extreme assumption could be relaxed by considering a flatter rate of return to skill in the illegal sector of the foreign country as compared to the labour market in the origin country, without changing the key insight of this Appendix.
illegal migration as a function of migration price $p$:

$$D^I(p) = \int_0^{\theta^I} f(\theta) d\theta = F(\theta^I)$$  \hspace{1cm} (27)

As $\theta^I$ decreases with $p$ and $w_h$ and increases with $d$ and $w_f$, it is easy to show that, once again, the demand for illegal migration is higher the lower the migration price, $p$, and the higher the wages differential $dw_f - w_h$ between the two countries.

We next study what happens if the government enters the migration market and sells visas. If returns to skill are higher in the legal sector of the destination country than in origin country legal migration will attract the highest skilled workers. Therefore, following the legalisation policy, a different pool of workers, who would not have migrated illegally otherwise, will decide to migrate legally. Moreover, there will be a large increase in the average skill level of migrants due to the positive selection of new immigrants through legal migration, who cross the border in addition to the pool of illegal migrants. It is this clear that the government cannot compete with the established smugglers using the policy instruments studied above, unless it proposes a price so low that it attracts all the workers.

So, if the aim of the policy is to eradicate human smuggling by attracting the demand from low skilled-workers while controlling migration flows, a more effective policy would be to sell visas to low skilled-workers only and the same reasoning as in the present paper would hence apply but at the bottom of the skill distribution.

In a more flexible model with intermediate selection of undocumented workers due to liquidity constraints (Borger 2011) and positive selection of legal workers the sale of visas should still be targeted at lower skill workers to be effective at pushing smugglers out of business.
8.2 Market Equilibrium and an illustration in the case of uniform distribution

We model the oligopolistic market for illegal migration as a generalized Cournot competition. We focus on symmetric equilibrium (i.e., each smuggler has the same market share). Let $D^I(Q) = (d w_f - w_h) F^{-1}(1 - Q)$ denote the inverse demand function for illegal migration. Smuggler $j = 1, ..., N$ maximises with respect to quantity $Q^j$ the profit function:

$$
\pi^j(Q^j, Q^{-j}) = [P^I(Q^j + Q^{-j}) - c] Q^j
$$

where $c$ represents the marginal costs for the smuggler and $Q^{-j} = \sum_{k \neq j} Q^k$ is the offer made by the competitors of $j = 1, ..., N$. The first order condition is sufficient under the assumption that the demand function is not too convex.

In a symmetric equilibrium $Q^j = \frac{Q}{N}$ and the generalized Cournot price with $N$ smugglers, $p^N$, is such that (3) holds.

We next illustrate the market equilibrium with the example of a uniform distribution of skills over $[0, 1]$, which gives easily tractable closed form solutions. From (1) and (2) we can write explicitly the demand for illegal migration as:

$$
D^I(p) = 1 - \frac{p}{d w_f - w_h}
$$

(28)

In the case of a generalized Cournot competition, we can use (3) to establish that the price is as follows:

$$
p^N = \frac{d w_f - w_h + N c}{N + 1}
$$

such that $p^m (= p^1) = \frac{d w_f - w_h}{2} + \frac{c}{2}$ and $p^\infty (= \lim_{N \to +\infty} p^N) = c$.

We deduce that the generalized Cournot demand is

$$
D^I(p^N) = \frac{N}{N + 1} \left( 1 - \frac{c}{d w_f - w_h} \right)
$$

Depending on the degree of competitiveness of the market, measured by $N$, the demand is between the demand on monopolistic market $D^I(p^m) = \frac{1}{2} - \frac{c}{2(d w_f - w_h)}$, and the demand in perfect competition $D^I(c) = 2D^I(p^m)$.
8.3 Proof of \( \frac{dp^I(p^L)}{dp^L} > 0 \)

To show that \( \frac{dp^I(p^L)}{dp^L} > 0 \) we totally differentiate (3) where the direct price elasticity of demand, which is derived from (8), is parameterized by \( p^L \).

We obtain that

\[
\frac{dp^I(p^L)}{dp^L} = -\frac{(p^I - c) \frac{\partial^2 D^I(p^I, p^L)}{\partial p^I \partial p^L} + \frac{1}{N} \frac{\partial D^I(p^I, p^L)}{\partial p^L}}{\frac{N+1}{N} \frac{\partial D^I(p^I, p^L)}{\partial p^I} + (p^I - c) \frac{\partial^2 D^I(p^I, p^L)}{\partial p^L^2}}
\]  

(29)

Second order condition of the oligopoly optimization problem implies that the denominator is negative. For instance with a uniform distribution it is easy to check that \( \frac{\partial^2 D^I(p^I, p^L)}{\partial p^I^2} = 0 \). Moreover we focus on a normal good so that \( \frac{\partial D^I(p^I, p^L)}{\partial p^I} < 0 \). A sufficient condition for the numerator to be positive is that \( \frac{\partial^2 D^I(p^I, p^L)}{\partial p^I \partial p^L} \geq 0 \). Using equation (8) we can easily show that this is always true as long as \( f'(\theta) \leq 0 \), which characterises for example the case with a uniform distribution (\( f'(\theta) = 0 \) over the support). It is also true when the density function is strictly decreasing as in developing countries where the vast majority of people do not have any education and are thus low skilled.QED

8.4 Uniform Distribution Example for Proposition 2

This section develops Proposition 2 in the case of a uniform distribution of skills distributed over 0 and 1. The demand faced by the smugglers when the government proposes a (legal) migration price, \( p^L \), is:

\[
D^I(p^I, p^L) = \int_{\frac{p^L - p^I}{w_f - w_h}}^{\frac{p^I}{w_f - w_h}} f(\theta) d\theta = \int_{\frac{p^L - p^I}{w_f - w_h}}^{\frac{p^I}{w_f - w_h}} d\theta = \frac{p^I - p^L}{(1-d)w_f} - \frac{p^I}{dw_f - w_h}
\]  

(30)

We deduce that the inverse demand function faced by the smugglers is:

\[
P^I(Q, p^L) = \frac{dw_f - w_h}{w_f - w_h} (p^L - (1-d)w_f Q)
\]  

(31)

Smuggler \( j = 1, \ldots, N \) maximises with respect to \( q^j \) the profit function:

\[
\pi^j(q^j, Q^{-j}) = [P^I(q^j + Q^{-j}, p^L) - c] q^j
\]

where \( c \) represents the marginal costs for the smuggler and \( Q^{-j} = \sum_{k \neq j} q^k \) is the offer made by the competitors of \( j = 1, \ldots, N \). In a symmetric equilibrium
\[ q^i = \frac{Q}{N} \] so that the Cournot quantity \( Q^N \) is such that:

\[
P^I(Q^N, p^L) - c + \frac{\partial P^I(Q^N, p^L)}{\partial Q^N} \frac{Q^N}{N} = 0 \tag{32}
\]

Symmetrically the generalized Cournot price with \( N \) smugglers, \( p^N \), is such that:

\[
\frac{p^N - c}{p^N} = \frac{1}{N} \frac{1}{\varepsilon_{D^I, p^I}} \tag{33}
\]

Second order condition requires that

\[
\frac{\partial^2 P^I(Q, p^L)}{\partial Q^2} \frac{Q}{N} + 2 \frac{\partial P^I(Q, p^L)}{\partial Q} \leq 0 \tag{34}
\]

which is always true with the uniform distribution example (see (31)).

Substituting (31) in the equation (32) we deduce that

\[
Q^N(p^L) = \frac{N}{N + 1} \left( p^L - c \frac{w_f - w_h}{w_f - w_h} \right) \frac{1}{(1 - d)w_f} \tag{35}
\]

or, alternatively, that

\[
P^N(p^L) = P^I(Q^N(p^L), p^L) = \frac{p^L}{N + 1} \frac{dw_f - w_h}{w_f - w_h} + \frac{N}{1 + N} c \tag{36}
\]

We now turn to showing that such反应 smugglers price is smaller than the price imposed by the smugglers under unconstrained oligopoly. With the uniform distribution example, replacing (10) into (13) the upper limit for the visa price satisfies:

\[
\bar{p}^L = [Nc + (1 + N)(1 - d)w_f] \frac{w_f - w_h}{(1 - d)w_f + N(w_f - w_h)} \tag{37}
\]

Comparing the reaction smugglers price \( p^I(\bar{p}^L) \) with the unconstrained smugglers’ oligopoly price \( p^N = \frac{dw_f - w_h + Nc}{N + 1} \) defined in (4) it is straightforward to check that \( p^I(\bar{p}^L) \leq p^N \) if and only if \( dw_f - w_h \geq c \), which is a necessary condition for the smugglers to be active in the first place. Indeed from (1), we obtain that: \( dw_f - w_h > p^I \) otherwise there is no illegal migrant. Moreover, necessarily \( c < p^I \) otherwise smugglers do not operate. Therefore, when smugglers operate, the condition \( c < dw_f - w_h \) is necessarily satisfied, which implies that \( p^I(\bar{p}^L) < p^N \). QED
8.5 Proof of Proposition 3

Let \( p^L(R_1, R_2) = \frac{w_f - w_h}{\alpha(R_2)w_f - w_h} c(R_1) \) be the price which pushes smugglers out of business and let \( D^L(R_1, R_2) = 1 - F\left( \frac{p^L(R_1, R_2)}{w_f - w_h} \right) \) the legal demand for visas associated with this price. The problem (17) the government aims to solve is equivalent to:

\[
\max_{R_1, R_2} p^L(R_1, R_2) \quad \text{s.t.} \quad R_1 + R_2 \leq D^L(R_1, R_2)p^L(R_1, R_2) \quad (38)
\]

The Lagrangian of this optimization problem is:

\[
L = p^L(R_1, R_2) + \lambda \{ D^L(R_1, R_2)p^L(R_1, R_2) - (R_1 + R_2) \} \quad (39)
\]

The Lagrangian derivatives are for \( k = 1, 2 \):

\[
\frac{\partial L}{\partial R_k} = \frac{\partial p^L}{\partial R_k} \left( 1 + \lambda D^L(R_1, R_2) \right) + \lambda p^L(R_1, R_2) \frac{\partial D^L}{\partial R_k} - \lambda \quad (40)
\]

Focusing on interior solutions, the optimal combination of \((R_1, R_2)\) satisfies necessarily \( \frac{\partial L}{\partial R_k} = \frac{\partial L}{\partial R_2} \), which yields:

\[
\frac{\partial p^L}{\partial R_2} \left( 1 + \lambda D^L(R_1, R_2) \right) + \lambda p^L(R_1, R_2) \frac{\partial D^L}{\partial R_2} = \frac{\partial p^L}{\partial R_1} \left( 1 + \lambda D^L(R_1, R_2) \right) + \lambda p^L(R_1, R_2) \frac{\partial D^L}{\partial R_1}
\]

Simplifying this expression by noting that \( \frac{\partial D^L}{\partial R_k} = -\frac{\partial}{\partial R_k} \left( \frac{w_f - w_h}{w_f - w_h} f \left( \frac{p^L(R_1, R_2)}{w_f - w_h} \right) \right) \), the optimal combination of \((R_1, R_2)\) is such that \( \frac{\partial p^L}{\partial R_1} = \frac{\partial p^L}{\partial R_2} \), which yields equation (19). The Lagrangian derivative with respect to \( \lambda \) yields equation (18). We now check with a simple example that the set of functions supporting an interior solution is not empty.

An example:

Let’s assume that \( w_h \approx 0 \) and that \( c(R) = c \frac{1 + 2R}{1 + R} \) and \( d(R) = \frac{d}{1 + R} \). Consistently with the model assumptions \( c(R) \) is increasing and concave and \( d(R) \) is decreasing and convex. Let’s note \( k(R) = \frac{c'(R)}{c(R)} = \frac{1}{(1 + R)(1 + 2R)} \) and let \( g(R) = \frac{d'(R) - R}{d(R - R)} = \frac{1}{1 + R - R} \) for all \( R \in [0, R] \) with \( R \) being a fixed point such
that $\tilde{R} = D^L(R, \tilde{R} - R) p^L(R, \tilde{R} - R)$. The interior solution of our problem is determined by that: $k(R) = g(R)$.\(^{40}\)

$$R_2^\ast(\tilde{R}) = \tilde{R} - R_1^\ast(\tilde{R}) = \tilde{R} + 1 - \sqrt{1 + \frac{\tilde{R}}{2}} \quad (41)$$

It is easy to check that both $R_1^\ast(\tilde{R})$ and $R_2^\ast(\tilde{R})$ take their value between $[0, \tilde{R}]$. They constitute an interior solution of the optimisation problem.

Let $p^L(\tilde{R}) = p^L(R_1^\ast(\tilde{R}), R_2^\ast(\tilde{R}))$ and $D^L(\tilde{R}) = D^L(R_1^\ast(\tilde{R}), R_2^\ast(\tilde{R}))$. To complete the proof we need to show that there exists a fixed point, $\tilde{R} > 0$, such that $\tilde{R} = D^L(\tilde{R}) p^L(\tilde{R})$.

The assumption $w_h \simeq 0$ implies that $p^L(\tilde{R}) = \frac{c(R_1^\ast)}{d(R_2^\ast)} = \frac{1 + 2 R_2^\ast}{1 + R_1^\ast}(1 + R_2^\ast)$. Substituting $R_1^\ast$ and $R_2^\ast$ by their value from (41) and rearranging the expression we get

$$p^L(\tilde{R}) = \frac{c^2}{d^2} \left( \sqrt{2(2 + \tilde{R})} - 1 \right)^2 \quad (42)$$

We deduce that $\tilde{R}$ is the solution to:

$$R = \frac{c}{d} \left( \sqrt{2(2 + \tilde{R})} - 1 \right)^2 \left( 1 - \frac{c}{dw_j \tilde{\theta}} \left( \sqrt{2(2 + \tilde{R})} - 1 \right)^2 \right) \quad (43)$$

The demand is defined if $1 \geq \frac{c}{dw_j \tilde{\theta}} \left( \sqrt{2(2 + \tilde{R})} - 1 \right)^2$, which is equivalent to $R \leq R^{max} = 0.5 \left( 1 + \sqrt{\frac{dw_j \tilde{\theta}}{c}} \right)^2 - 2$. We deduce that $R^{max} > 0$ if and only if

$$\frac{dw_j \tilde{\theta}}{c} > 1 \quad (44)$$

Note that this assumption is always verified whenever there is some human smuggling: $c < dw_j \tilde{\theta}$. Therefore $R^{max} > 0$ and it is straightforward to check that $\tilde{R}$ exists. Indeed when $R = 0$ the left hand side of equation (43) is equal to $LHS(0) = 0$, while the right hand side is equal to $RHS(0) = \frac{c}{d} \left( 1 - \frac{c}{dw_j \tilde{\theta}} \right) > 0$ under (44). Symmetrically the left hand side of equation (43) when $R = R^{max}$ is equal to $LHS(R^{max}) = R^{max} > 0$ under (44), while $RHS(R^{max}) = 0$.

\(^{40}\)It is easy to check that $k'(R) < 0$ and that $g'(R) > 0 \forall R \in [0, \tilde{R}]$. Since $k(R)$ is strictly decreasing and $g(R)$ is strictly increasing for all $R \in [0, \tilde{R}]$, and since $g(0) < k(0)$, and $g(\tilde{R}) > k(\tilde{R}) \forall \tilde{R} > 0$, there exists an unique interior solution to $k(R) = g(R)$. 48
Since both functions are continuous they cross necessarily at least once at $R \in (0, R^{\text{max}})$.

Moreover, after noting that:

$$RHS'_0(R) = 2 \frac{c}{d} \left[ \frac{\sqrt{2(2 + R)} - 1}{\sqrt{2(2 + R)}} \right] \left\{ 1 - \frac{c}{dwf} \frac{2(\sqrt{2(2 + R)} - 1)^2}{d} \right\}$$

we can check that $RHS'_0(R) < 0 \iff dwf > 2c(\sqrt{2(2 + R)} - 1)^2$, which is for instance true if $2 > \frac{dwf}{c} > 1$. In this case the function $LHS(.)$ is increasing and $RHS(.)$ is decreasing: they cross only once. QED

8.6 Risk aversion

Proof of Lemma 1

Applying the expected utility theorem and comparing the individual’s expected utility in case he/she migrates, equal to $(1 - q)u(\theta \delta w_f - p^I) + qu(\theta w_h - p^I)$ with the expected utility in case she does not migrate, equal to $u(\theta w_h)$, we can write the migration condition as: $u(\theta w_h) < (1 - q)u(\theta \delta w_f - p^I) + qu(\theta w_h - p^I)$. Studying the threshold such that an individual is just indifferent between migrating illegally or not migrating, the marginal type $\theta^I_{ra}$ is the solution of the following equation: $u(\theta w_h) = (1 - q)u(\theta \delta w_f - p^I) + qu(\theta w_h - p^I)$. Substituting $u(x) = 1 - \exp(-ax)$ and rearranging this expression, we obtain the illegal migration threshold $\theta^I_{ra}$ as a solution of the equation (21): $\frac{1 - e^{-ap^I}}{1 - e^{-ap^I} + \theta w_h} = 1 - q$.

Let $\nu(\theta) = \frac{1 - e^{-ap^I}}{1 - e^{-ap^I} + \theta w_h}$. Deriving twice the function $\nu(\theta)$ one can easily check that it is decreasing and convex in $\theta$. Moreover $\lim_{\theta \to 0} \nu(\theta) = +\infty$ and $\lim_{\theta \to -\infty} \nu(\theta) = 1 - e^{-ap^I}$. We deduce, first, that if $q$ is strictly lower than $e^{-ap^I}$ then $\theta^I_{ra}$ exists and is unique and, second, that $\theta^I_{ra}$ is increasing with $q$.

We can write the demand for illegal migration as a function of the migration price $p^I$ similarly as before, except that $\theta^I$ is now replaced by $\theta^I_{ra}$:

$$D^I_{ra}(p^I) = \int_{\theta^I_{ra}}^{\theta^I} f(\theta)d\theta = 1 - F(\theta^I_{ra}) \quad (45)$$
As \( \theta_{ra}^I \) increases with \( p^I \) and decreases with \( \delta \), the demand for migration remains higher the lower the migration price, \( p^I \), and the higher the wages differential \( \delta w_f - w_h \) between the two countries. The logic of the pricing scheme of smugglers described in section 2 remains thus the same as before but it takes into account the new (lower) demand from risk averse individuals (45).

We now formally show in the uniform example that risk aversion implies that the price imposed by smugglers is then lower than the price they would impose to risk neutral individuals with the same expected revenue from migration. With risk neutrality we have \( \theta^I(p) = \frac{p}{dw_f - w_h} \) and

\[
D^I(p) = \int_{\theta^I}^{1} f(\theta)d\theta = 1 - F(\theta^I) = 1 - \theta^I(p) \tag{46}
\]

We deduce that the (absolute value) of the price elasticity of demand is:

\[
\varepsilon_{D,p} = \frac{-D^{I'}(p)p}{D^I(p)} = \frac{\theta^I(p)}{1 - \theta^I(p)} = \frac{p}{(dw_f - w_h) - p}
\]

With risk aversion, we have \( \theta_{ra}^I \) which is such that:

\[
1 - e^{-\alpha p} \frac{1}{1 - e^{-\alpha(\delta w_f - w_h)}} = 1 - q \tag{47}
\]

We deduce that:

\[
\theta_{ra}^I(p) = \frac{\log(1 - q) - \log(e^{-\alpha p} - q)}{\alpha(\delta w_f - w_h)} \tag{48}
\]

the demand is:

\[
D_{ra}^I(p) = \int_{\theta_{ra}^I}^{1} f(\theta)d\theta = 1 - F(\theta_{ra}^I) = 1 - \theta_{ra}^I(p) \tag{49}
\]

It is straightforward to check that if \( q = 0 \) (i.e., there is no risk of deportation in migrating illegally) then \( \delta = \delta \) so that \( \theta_{ra}^I(p) = \theta^I(p) \).

We deduce that the (absolute value) of the price elasticity of demand is:

\[
\varepsilon_{D_{ra},p} = \frac{-D_{ra}^{I'}(p)p}{D_{ra}^I(p)} = \frac{p e^{-\alpha p}}{(\delta w_f - w_h) - \log(1 - q) - \log(e^{-\alpha p} - q)} \tag{50}
\]

Here again it is easy to check that \( \varepsilon_{D_{ra},p} = \varepsilon_{D,p} \) when \( q = 0 \). After differentiating \( \varepsilon_{D_{ra},p} \) with respect to \( q \leq 1 \) and noting that \( a(\delta w_f - w_h) - \log(1 - q) + \log(e^{-\alpha p} - q) \)
q) > 0 as 0 < \theta^L_{ra}(p) < 1 one can check that \varepsilon_{D_{ra,p}} increases with q:
\[
\frac{d\varepsilon_{D_{ra,p}}}{dq} \equiv \left( a(\delta w_f - w_h) - \log(1 - q) + \log (e^{-ap} - q) \right) + \frac{1 - e^{-ap}}{1 - q} > 0 \tag{51}
\]
So when the risk q augments the demand price elasticity increases, and thus, everything else being equal, the monopoly price is lower. QED

**Proof of Lemma 2**

We now turn to the government policy of visa sale and the reaction of smugglers. If individuals can buy a legal permit to migrate at price \( p^L \), smugglers need to price their services low enough so that at least one individual wishes to migrate illegally. The skill level \( \theta^L_{ra} \) of the marginal illegal migrant who is just indifferent between migrating illegally and legally satisfies \( u(\theta w_f - p^L) = (1 - q)u(\delta w_f - p^l) + qu(\theta w_h - p^l) \). Substituting \( u(x) = 1 - \exp(-ax) \) and rearranging this expression, we obtain the legal migration threshold \( \theta^L_{ra} \) as a solution of the following equation:
\[
\frac{1 - e^{-a(\theta(w_f - w_h) + p^l - p^L)}}{1 - e^{-a(\delta w_f - w_h)}} = 1 - q \tag{52}
\]
Solving for the threshold \( \theta^L_{ra} \) and comparing it to (6) we show in the following that \( \theta^L_{ra} < \theta^L \).

**Proof.** Let \( \rho(\theta) = \frac{1 - e^{-a(\theta(w_f - w_h) + p^l - p^L)}}{1 - e^{-a(\delta w_f - w_h)}} \). Equation (52) defines \( \theta^L_{ra} \) as a solution of \( \rho(\theta) = 1 - q \). The benchmark case of risk neutrality is obtained by setting \( q = 0 \) in this equation. Indeed when \( q = 0 \) and \( \delta = d \) the unique solution of \( \rho(\theta) = 1 \) is \( \theta^L \) defined equation (6). This also implies that the function \( \rho(\theta) \) crosses once and only once the horizontal line 1.

Next, deriving \( \rho(\theta) \) with respect to \( \theta \) yields:
\[
\rho'(\theta) = \frac{a(1 - e^{-a(\theta(w_f - w_h) + p^l - p^L)})}{1 - e^{-a(\delta w_f - w_h)}} \times \left\{ \frac{(w_f - w_h)e^{-a(\theta(w_f - w_h) + p^l - p^L)}}{1 - e^{-a(\theta(w_f - w_h) + p^l - p^L)}} - \frac{(\delta w_f - w_h)e^{-a(\delta w_f - w_h)}}{1 - e^{-a(\delta w_f - w_h)}} \right\}
\]
To study the sign of \( \rho'(\theta) \) we consider 2 cases:
• If $\theta \leq \frac{p^L - p^I}{w_f - w_h}$ then $\theta(w_f - w_h) + p^I - p^L \leq 0$ so that $1 - e^{-a(\theta(w_f - w_h) + p^I - p^L)} \leq 0$. Since by assumption $w_f - w_h \geq \delta w_f - w_h \geq 0$ all the other elements in the fractions composing $\rho'(\theta)$ are positive. We deduce that both the first term and the term in the brackets are negative such that $\rho'(\theta) > 0$.

• If $\frac{p^L - p^I}{w_f - w_h} < \theta \leq \frac{p^L - p^I}{(1 - \delta)w_f}$ then $0 < \theta(w_f - w_h) + p^I - p^L \leq \theta(\delta w_f - w_h)$ and $1 - e^{-a(\theta(w_f - w_h) + p^I - p^L)} > 0$. Since $1 - e^{-ax}$ is log concave in $x$, we have that $\frac{e^{-a(\theta(w_f - w_h) + p^I - p^L)}}{1-e^{-a(\theta(w_f - w_h) + p^I - p^L)}} \geq \frac{e^{-a(\delta w_f - w_h)}}{1-e^{-a(\delta w_f - w_h)}}$. Moreover we have $w_f - w_h \geq \delta w_f - w_h \geq 0$ such that the term in the brackets is now positive.

Similarly the first term is also now positive such that $\rho'(\theta) > 0$.

We have just shown that the continuous function $\rho(\theta)$ is increasing for $\theta \in [0, \theta^L]$. Moreover it crosses once and only once the horizontal line at $q = 0$ for $\theta = \theta^L$. We deduce that for $\theta > \theta^L$, $\rho(\theta) > 1$ so that equation (52) never holds.

The relevant domain for $\theta^L_{ra}$ in equation (52) when $q$ varies between 0 and 1 is $\theta \in [0, \theta^L]$. This implies that if $\theta^L_{ra}$ exists it is necessarily such that $\theta^L_{ra} \leq \theta^L$ with a strict inequality for any $q > 0$.

To finish the proof of Lemma 2 we need to show that $\theta^L_{ra}$ exists and is unique. It is done by noting that $\lim_{\theta \to -0} \rho(\theta) = -\infty$. So the function $\rho(\theta)$ strictly increases between $-\infty$ and 1 when $\theta$ varies between 0 and $\theta^L$. It necessarily crosses the line $q \in [0, 1]$ once and only once.QED

Proof of Lemma 3

In order to eradicate the smugglers we know that

$$\theta^L_{ra}(c) = \theta^L_{ra}(c, p^L_{ra})$$

(53)

with $\theta^L_{ra}(c) = \frac{\log(1-q) - \log(e^{-c} - q)}{a(\delta w_f - w_h)}$.

Moreover, from (21) $\theta^L_{ra}(c, p^L_{ra})$ is the implicit solution of

$$1 - q = \frac{1 - e^{-a(\theta(w_f - w_h) + e - p^L_{ra})}}{1 - e^{-a(\delta w_f - w_h)}}$$
This implies that $p^L_{ra}$ satisfies the following equation

$$(1 - q) (1 - e^{-a(\delta w_f - w_h)}) = 1 - e^{-a(\theta(w_f - w_h) + c - p^L_{ra})}$$

with $\theta = \theta_{ra}(c) = \frac{\log(1 - q) - \log(e^{-ca} - q)}{a(\delta w_f - w_h)}$

This yields successively that:

$$c = \theta_{ra}(c) (w_f - w_h) + c - p^L_{ra}$$

$$p^L_{ra} = \frac{\log(1 - q) - \log(e^{-ca} - q)}{a(\delta w_f - w_h)} (w_f - w_h) \tag{54}$$

and we can check easily that $dp^L_{ra}/dq > 0$. QED

The reasoning of section 3.2.2 remains valid under risk aversion. The IR constraint, which can be written $1 - e^{-a(\bar{\sigma} w_f - p^L_f)} \geq 1 - e^{-a\bar{\sigma} w_h}$, is unchanged.

The IC constraint becomes $1 - e^{-a(\bar{\sigma} w_f - p^L_f)} \geq (1 - q) \left(1 - e^{-a(\delta w_f - p^L_f)} + q(1 - e^{-a(\bar{\sigma} w_f - p^L_f)})\right)$. The IC constraint is binding if $(1 - q) \left(1 - e^{-a(\delta w_f - p^L_f)} + q(1 - e^{-a(\bar{\sigma} w_f - p^L_f)})\right) \geq 1 - e^{-a\bar{\sigma} w_h}$, which is a necessary condition for the smuggler to be active. So if the smuggler is active the binding constraint is the IC and $p^L_{ra}$ is the solution of the following equation:

$$e^{-a(\bar{\sigma} w_f - p^L_f)} = (1 - q) e^{-a(\delta w_f - p^L_{ra}(p^L_f))} + q e^{-a(\bar{\sigma} w_f - p^L_{ra}(p^L_f))}$$

**Proof of Proposition 4**

Using three instruments to eradicate human smuggling while controlling migration flows, the government solves:

$$\max_{R_1, R_2, R_3} p^L(R_1, R_2, R_3) \text{ s.t. } R_1 + R_2 + R_3 \leq D^L(R_1, R_2, R_3) p^L_{ra}(R_1, R_2, R_3) \tag{55}$$

The Lagrangian of this optimization problem is:

$$L = p^L(R_1, R_2, R_3) + \lambda \left\{D^L(R_1, R_2, R_3) p^L_{ra}(R_1, R_2, R_3) - (R_1 + R_2 + R_3) \right\} \tag{56}$$

The Lagrangian derivatives are for $k = 1, 2, 3$:

$$\frac{\partial L}{\partial R_k} = \frac{\partial p^L}{\partial R_k} \left(1 + \lambda D^L(R_1, R_2)\right) + \lambda p^L_{ra}(R_1, R_2) \frac{\partial D^L}{\partial R_k} - \lambda \tag{57}$$
Focusing on interior solutions, the optimal combination of \((R_1, R_2, R_3)\) satisfies necessarily: \(\frac{\partial L^L}{\partial R_1} = \frac{\partial L^L}{\partial R_2} = \frac{\partial L^L}{\partial R_3}\). Simplifying this expression by noting that \(\frac{\partial L^L}{\partial R_n} = -\frac{\partial p^L}{w_f - w_h} f \left( \frac{p^L(R_1, R_2, R_3)}{w_f - w_h} \right)\) yields that the optimal combination is such that \(\frac{\partial p^L}{\partial R_1} = \frac{\partial p^L}{\partial R_2} = \frac{\partial p^L}{\partial R_3}\), which yields equation (25). Moreover the Lagrangian derivative with respect to \(\lambda\) yields equation (24). QED

**Link with Becker (1968)**

Assuming to simplify that \(w_h = 0\) we can determine the investments such that expected earnings from illegal migration, \((1 - q(R_3))\delta(R_2)w_f + q(R_3)w_h = (1 - q(R_3))\delta(R_2)w_f\), are minimized under the budget constraint \(R_2 + R_3 = \bar{R}\). As \(R_2 = \bar{R} - R_3\), \(R_3\) is the solution to:

\[
-\frac{\delta'(\bar{R} - R_3)}{\delta(\bar{R} - R_3)} = \frac{q'(R_3)}{1 - q(R_3)}
\]

(58)

Under the assumption that the functions \(1 - q(R)\) and \(\delta(R)\) are log convex, which is for instance the case when \(q(R) = 1 - q/(1 + R)\) and \(\delta(R) = \delta/(1 + R)\), the function \(f(R) = \frac{\delta'(R)}{1 - q(R)}\) decreases with \(R\) and the function \(g(R) = \frac{-\delta'(\bar{R} - R)}{\delta(\bar{R} - R)}\) increases with \(R\). Under the assumption that \(f(0) > g(0)\) and \(f(\bar{R}) < g(\bar{R})\) then \(R^*_{3n}\) solution of (58) exists and is unique. When for instance \(q(R) = 1 - q/(1 + R)\) and \(\delta(R) = \delta/(1 + R)\) then \(g(R) = \frac{1}{\bar{R} - R}\) and \(f(R) = \frac{1}{1 + R}\). This implies \(f(0) = 1 > g(0) = \frac{1}{\bar{R} - R}\) and \(f(\bar{R}) = \frac{1}{1 + R} < g(\bar{R}) = 1\) so that \(R^*_{3n} = \bar{R}/2\). This determines the optimal allocation of investment between the two instruments to reduce migration flows under the assumption of risk neutrality.

However, if individuals are risk-averse, minimizing the flow of migrants is not equivalent to minimizing expected earnings of would be migrants. Using our model, minimizing the flow of migrants is equivalent to maximizing the price of visas, which can be written as

\[
\frac{L^L}{\gamma(R_3)} = \frac{\log(1 - q(R_3)) - \log(\gamma(R_3))}{\alpha b(R - R_3)w_f} (w_f - w_h).
\]

Assuming again to simplify that \(w_h = 0\), we can rewrite the price \(\frac{L^L}{\gamma(R_3)} = \frac{\log(1 - q(R_3)) - \log(\gamma(R_3))}{\alpha b(R - R_3)w_f}\) and maximise it with respect to \(R_3\) with the constraint that \(R_3 + R_2 = \bar{R}\).
We find that
\[
\frac{\partial q^{L}}{\partial R} = \frac{1}{a\delta(R - R) - R_3} \left\{ \frac{q'(R) - 1 - q(R)}{e^{-ca} - q(R)} - 1 \right\} + \frac{\delta'(R - R_3)}{\delta(R - R_3)} \left[ \log(1 - q(R)) - \log(e^{-ca} - q(R)) \right]
\]
Under risk aversion an interior solution of our problem is such that \(\partial q^{L} / \partial R_3 = 0\), which determines implicitly the optimal investment \(R_3^{ca}\) as solution of the following equation:
\[
-\delta'(R - R_3) = \frac{q'(R)}{1 - q(R_3)} \frac{1 - q(R_3)}{e^{-ca} - q(R_3)} - 1 \frac{\log(1 - q(R)) - \log(e^{-ca} - q(R))}{(59)}
\]
By comparing (58) and (59) it is easy to see that the investment to increase the probability of deportation is higher under risk aversion than under risk neutrality: \(R_3^{ca} > R_3^{rn}\). Indeed, since \(f(R) = \frac{q'(R)}{1 - q(R)}\) decreases and \(g(R) = \frac{-\delta'(R - R_3)}{\delta(R - R_3)}\) increases with \(R\), \(R_3^{ca} > R_3^{rn}\) if the function \(f(R)\) is shifted to the right (i.e., if it increases). This depends on the distortion in (59) being greater than 1, which is equivalent to:
\[
\frac{1 - q(R_3)}{e^{-ca} - q(R_3)} - 1 > \log \left( \frac{1 - q(R_3)}{e^{-ca} - q(R_3)} \right) \quad (60)
\]
Since \(\frac{1 - q(R_3)}{e^{-ca} - q(R_3)} > 1\) this is always true (i.e., \(x - \log x - 1 > 0 \quad \forall x > 1\)). We have thus established that \(q(R_3^{rn})\) is lower than the probability of deportation \(q(R_3^{ca})\), which minimises migration flows.QED

8.7 Rationality of migration decisions

This Appendix departs from the estimated prices paid by Chinese illegal migrants to go to the US, which have been documented in Friebel and Guriev, 2006 and previous work to be above $35000 in mid 1990s and then continued to rise and checks that the rationality constraint of our model is satisfied for the wages differential between the US and China observed in 2005 and for a large range of wage differentials observed between advanced and developing countries.

To calibrate \(d\), we use Cobb-Clark and Kossoudji’s (2002) estimates of 14 to 24% legalisation premia which, we round at 20%. Assuming \(d = 0.8\) is also
in line with the findings of Rivera-Batiz (1999) on the gap in wages differential between legal and undocumented immigrants on the US market, which remains unexplained by differences in measured characteristics of these two groups.\footnote{Although these estimates are based on Mexican immigrants and may be different for long-distance illegal migrants, who may come from very different areas such as South East Asia, Russia or Africa and may have different skill distributions, these are, to our knowledge, the best available proxies.}

To calculate the net present value of working illegally in the US we follow Friebel and Guriev, 2006, and take the average minimum wages in the US, $6.15 per hour, and assume that a migrant works 45 hours for 52 weeks per year over a period of 40 years. Accordingly, assuming the discount and growth rates of future wages are equal and without loss of generality setting it to zero, NPV of earnings in the US is around $575640 ($= 52 \cdot 45 \cdot $6.15 \cdot 40$). Moreover, estimates of the GDP per capita in China in terms of purchasing power are in the range of $4000 such that, over 40 years, the NPV of earnings in China are estimated around $160000 ($= $4000 \cdot 40$).\footnote{This estimate of GDP per capita reported by the CIA World Factbook 2005 corresponds to a wage equal to 1.7 dollar per hour in China, which, given the adjustment by the differential in purchasing power between China and the US, does not seem unreasonable. See https://www.cia.gov/library/publications/the-world-factbook/}

We can check that the IR constraint, $p^I \leq (d w_f - w_h)$, is largely satisfied (as $p^I < 575640 \cdot 0.8 - 160000$) for the case of the Chinese migration to the US.

More generally, we check that the constraint $p^I \leq w_h (d w_f - w_h)$ is easily satisfied for a large range of ratios $\frac{w_f}{w_h}$ ($=2, 3, 4, 5, 7, 10, 15, and 25$) based on wage differentials between advanced and developing countries reported by Freeman et al. (2000) or on purchasing power adjusted wages ratios computed by Clemens et al. (2009) for workers who are otherwise observably identical. However, since we do not have good estimates for the prices to cross illegally from one origin to another destination country, we prefer to focus on the illegal Chinese migration to the US for the remainder of our simulations.

### 8.8 Risk aversion and probability of deportation

From the Cournot Price (3) and replacing the price elasticity of the demand for migration $\varepsilon_{D, a, p}$ using our calculations above (50) we can write the marginal
costs for smugglers to operate, $c_{ra}$, as follows:

\[
c_{ra} = p^I - \frac{1}{N} (\delta w_f - w_h) - \frac{\log(1-q) - \log(e^{-ap^I} - q)}{a} \left( \frac{e^{-ap^I}}{e^{-ap^I} - q} \right)
\]

(61)

Replacing in (61) with $p^I = 35000$, $\delta = 0.8$, $w_f = 575640$, $w_h = 160000$, $N = 2$, and $c_{ra} = 10000$ we can determine a set of absolute risk aversion parameters $a$, which correspond to a set of deportation probabilities $q$.

To illustrate the magnitude of the policy implications of the model, we present our results for four sets of compatible values $(0.7, 0.00000086)$, $(0.5, 0.00001)$, $(0.4, 0.00002)$, $(0.2, 0.000039)$.

8.9 Simulations

8.9.1 Increase in demand following legalisation

Assuming a uniform distribution over $[0, 1]$ the demand for illegal migration in the absence of legalisation is: $D^I_{ra}(p^I) = 1 - \theta^I_{ra}$, with $\theta^I_{ra}$ solution of the equation (21), such that:

\[
D^I_{ra}(p^I) = 1 - \frac{\log(1-q) - \log(e^{-ap^I} - q)}{a(\delta w_f - w_h)}
\]

(62)

whereas, following the legalisation, the demand becomes

\[
D^L_{ra}(p^L_{ra}) = 1 - \frac{\log(1-q) - \log(e^{-ac} - q))}{a(\delta w_f - w_h)}
\]

(63)

For the values $(a, q)$ discussed above we can simulate the relative increase in migration demand following the policy as follows:

\[
\Delta D = \frac{D^L_{ra}(p^L_{ra}) - D^I_{ra}(p^I)}{D^I_{ra}(p^I)} = \frac{\log(e^{-ca} - q) - \log(e^{-ap^I} - q)}{a(\delta w_f - w_h) - \log(1-q) + \log(e^{-ap^I} - q)}
\]

8.9.2 Legalisation with migration control policy

Using the first instrument, $c$

After replacing in $D^I_{ra}(p^I) = D^L_{ra}(p^L_{ra})$ we find that $c(R^*)$ must satisfy the following equation:
\[ \frac{\log(1 - q) - \log \left( e^{-a p^f} - q \right)}{a (\delta w_f - w_h)} = \frac{\log(1 - q) - \log \left( e^{-ac(R^*)} - q \right)}{a (\delta w_f - w_h)} \]

which is equivalent to \( p^f = c(R^*) \).

**Varying the risk of deportation following the policy**

If the government invests in additional repression such that \( q^* = q(R_3) \), the required amount of additional efforts to keep constant the migration demand following the legalisation is such that:

\[ \frac{\log(1 - q) - \log \left( e^{-a p^f} - q \right)}{a (\delta w_f - w_h)} = \frac{\log(1 - q) - \log \left( e^{-ac(R^*)} - q^* \right)}{a (\delta w_f - w_h)} \]

which is equivalent to \( e^{-ac(R^*)} = \left( \frac{1 - q^*}{1 - q} \right) \left( e^{-a p^f} - q \right) + q^* \)

This shows that \( \partial c(R^*)/\partial q^* < 0 \).

We can hence compute the relative increase in marginal costs, or \( \Delta c = \frac{c(R^*) - c}{c} \), which is necessary to eliminate the smugglers without increasing the demand as a function of risk of deportation \( q^* \) and check that it decreases with \( q^* \).

**Using the second instrument, \( \delta \)**

Similarly, after replacing in \( D_{1a}(p^f) = D_h \left( p_{1a}^f(R^*) \right) \) we find that \( \delta(R^*) \) solution of the following equation

\[ \frac{\log(1 - q) - \log \left( e^{-a p^f} - q \right)}{a (\delta w_f - w_h)} = \frac{\log(1 - q^*) - \log \left( e^{-ac} - q^* \right)}{a (\delta(R^*) w_f - w_h)} \]

which is equivalent to:

\[ \frac{\delta(R^*) w_f - w_h}{\delta w_f - w_h} = \frac{\log \left( \frac{1 - q^*}{1 - q} \right)}{\log \left( \frac{1 - q}{e^{-ap^f} - q} \right)} \]

Using the solution of this equation we can compute \( \Delta \delta = \frac{\delta(R^*) - \delta}{\delta} \) and check that \( \Delta \delta \), which is negative, gets closer to zero as \( q^* \) increases.
8.9.3 Robustness checks: Varying the number of smugglers on the market

First we can check that the observations of a large differential between the migration price charged by smugglers (i.e., $p = 35000$) and the marginal cost (i.e., $c = 10000$) is not compatible with a relatively competitive market. The large markup suggests a cartelized smuggling market. For instance assuming $N = 10$ or above would imply, using equation (61), that deportation risk is below 0.05 which is not very realistic.

For our simulations above we assumed that $N = 2$. We now turn to testing the sensitivity of our results if the market for smugglers is characterised by $N = 3$ and $N = 5$ smugglers. Simulations presented in the tables A1 and A2 show the magnitude of the implied changes. Note that, similarly as above, the degrees of risk aversion and deportation probabilities displayed in the first two rows of each table have been chosen to be compatible with the observations $c = 10000$ and $p = 35000$ characterising the market for Chinese illegal migrants.
Tables

Table 1: Policy implications for N=2 when risk q varies for different degrees of risk aversion a.

<table>
<thead>
<tr>
<th>a</th>
<th>0.00000086</th>
<th>0.00001</th>
<th>0.00002</th>
<th>0.00004</th>
</tr>
</thead>
<tbody>
<tr>
<td>q</td>
<td>0.68</td>
<td>0.48</td>
<td>0.38</td>
<td>0.18</td>
</tr>
<tr>
<td>$p_{Lra}$</td>
<td>43624 0.7</td>
<td>28232 0.5</td>
<td>23785 0.4</td>
<td>17755 0.2</td>
</tr>
<tr>
<td>$\Delta D$</td>
<td>0.43</td>
<td>0.32</td>
<td>0.28</td>
<td>0.20</td>
</tr>
<tr>
<td>$\Delta c$</td>
<td>2.73</td>
<td>2.67</td>
<td>2.67</td>
<td>2.70</td>
</tr>
<tr>
<td>$\Delta \delta$</td>
<td>-0.48</td>
<td>-0.51</td>
<td>-0.52</td>
<td>-0.53</td>
</tr>
</tbody>
</table>

Note: prices $p_{Lra}$ are in USD

Tables in Appendix

Table A1: Policy implications for N=3 when risk q varies for different degrees of risk aversion a.

<table>
<thead>
<tr>
<th>a</th>
<th>0.000002</th>
<th>0.000008</th>
<th>0.000015</th>
<th>0.000035</th>
</tr>
</thead>
<tbody>
<tr>
<td>q</td>
<td>0.58</td>
<td>0.48</td>
<td>0.38</td>
<td>0.18</td>
</tr>
<tr>
<td>$p_{Lra}$</td>
<td>33361 0.6</td>
<td>27621 0.5</td>
<td>23429 0.4</td>
<td>17650 0.2</td>
</tr>
<tr>
<td>$\Delta D$</td>
<td>0.30</td>
<td>0.26</td>
<td>0.23</td>
<td>0.18</td>
</tr>
<tr>
<td>$\Delta c$</td>
<td>2.68</td>
<td>2.66</td>
<td>2.65</td>
<td>2.68</td>
</tr>
<tr>
<td>$\Delta \delta$</td>
<td>-0.48</td>
<td>-0.50</td>
<td>-0.52</td>
<td>-0.53</td>
</tr>
</tbody>
</table>

Note: prices $p_{Lra}$ are in USD

Table A2: Policy implications for N=5 when risk q varies for different degrees of risk aversion a.

<table>
<thead>
<tr>
<th>a</th>
<th>0.0000005</th>
<th>0.000005</th>
<th>0.000026</th>
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</thead>
<tbody>
<tr>
<td>q</td>
<td>0.44</td>
<td>0.38</td>
<td>0.18</td>
</tr>
<tr>
<td>$p_{Lra}$</td>
<td>24749 0.46</td>
<td>22658 0.4</td>
<td>17414 0.2</td>
</tr>
<tr>
<td>$\Delta D$</td>
<td>0.19</td>
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<td>0.15</td>
</tr>
<tr>
<td>$\Delta c$</td>
<td>2.63</td>
<td>2.63</td>
<td>2.64</td>
</tr>
<tr>
<td>$\Delta \delta$</td>
<td>-0.46</td>
<td>-0.48</td>
<td>-0.50</td>
</tr>
</tbody>
</table>

Note: prices $p_{Lra}$ are in USD
legal migration only

legal and illegal migration co-exist

unconstrained smugglers

Figure 1: Pricing scheme of the smugglers $p^I(p^L)$ in the uniform example